

## **Quantify transport errors in CO<sub>2</sub> mixing ratios using a small-size ensemble**

*Thomas Lauvaux, Penn State University*

**1. Generate a calibrated ensemble which represents the characteristics of transport errors using a minimum number of members**

*PhD of Liza Diaz-Isaac (now at Scripps, UC San Diego)*

**2. Remove the sampling noise due to the limited number of members**

*in collaboration with Marc Bocquet (CEREA, Paris) and Nicolas Boussez (U. of Colorado)*

# Physics-based ensemble of atmospheric simulations

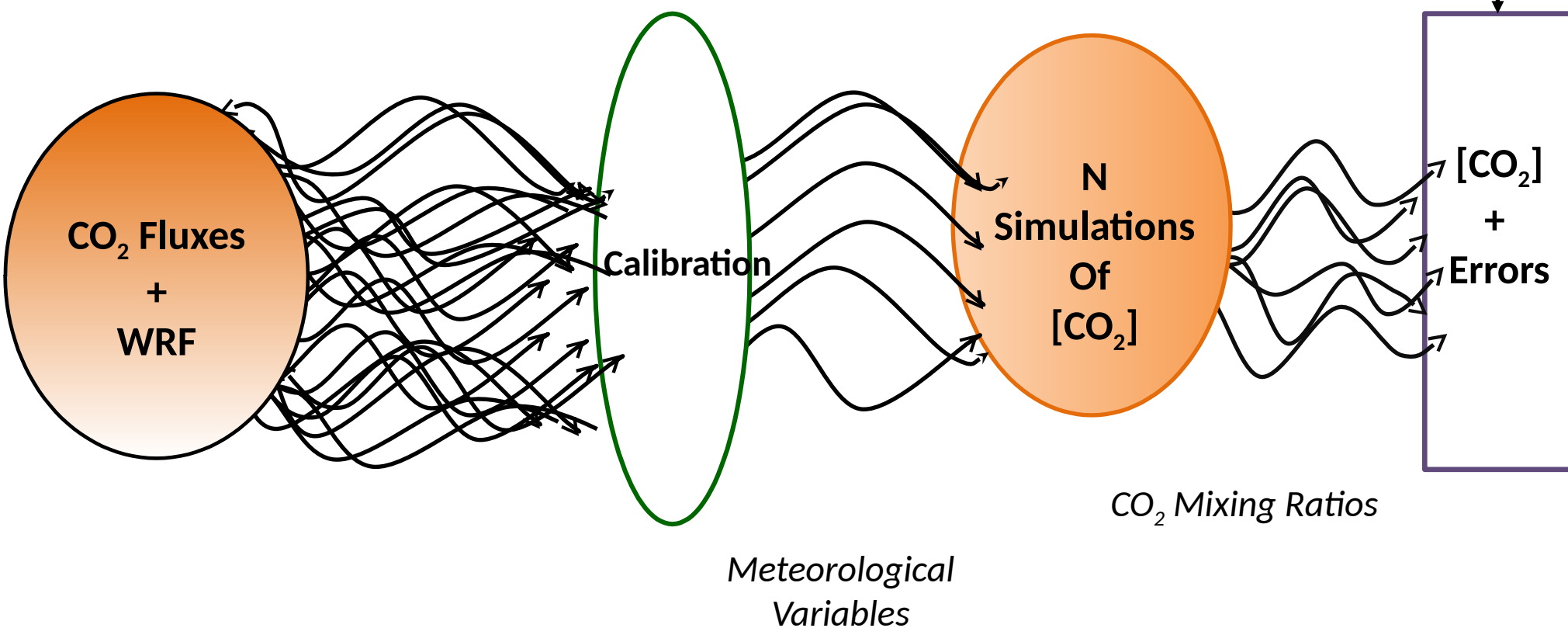
## Objective 1

Generate an ensemble of simulations using an atmospheric modeling system

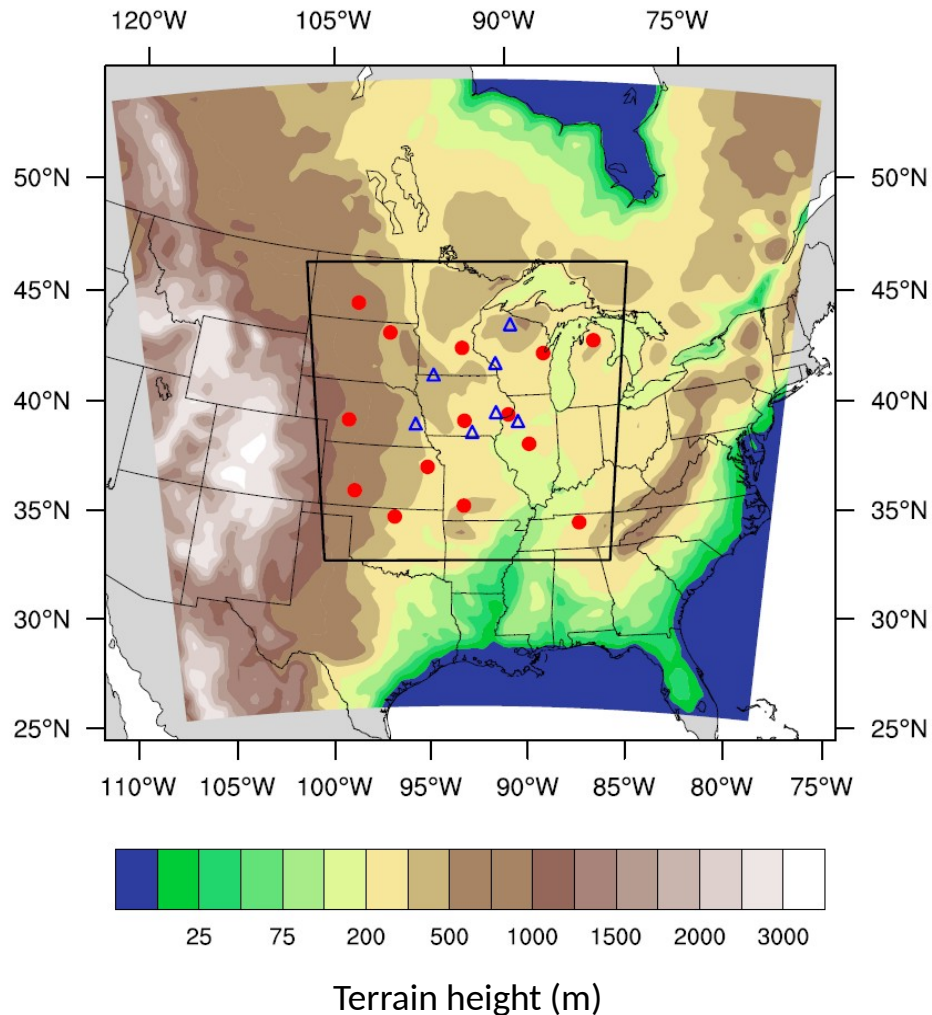
## Objective 2

Evaluate if the Ensemble Spread Represents the Transport Errors

Assess Transport Errors in the Atmospheric Inversion.



# Description of the WRF simulation domain



**Period:** June 18-July 21, 2008

**Grid Resolution:**

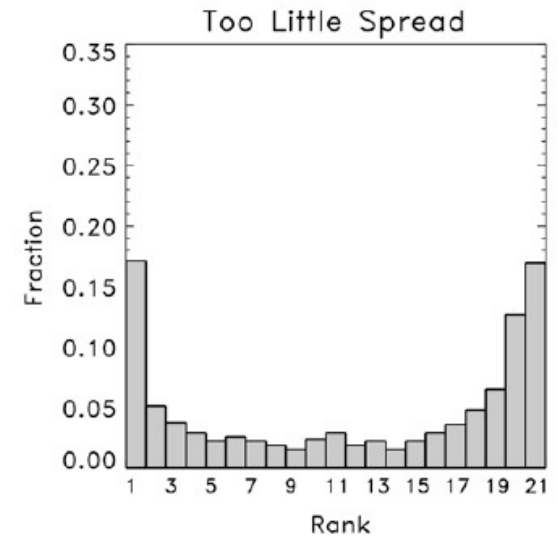
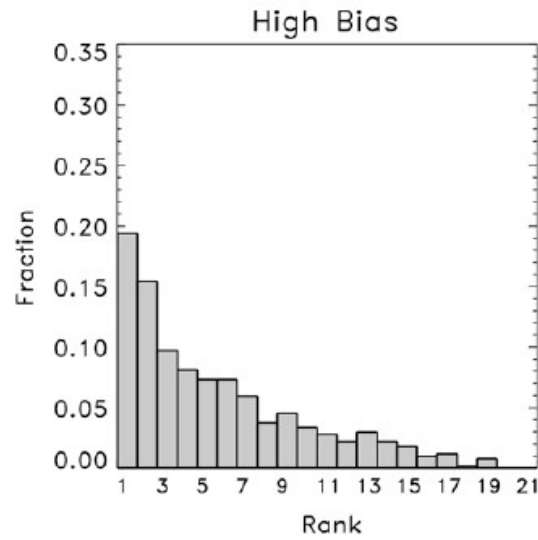
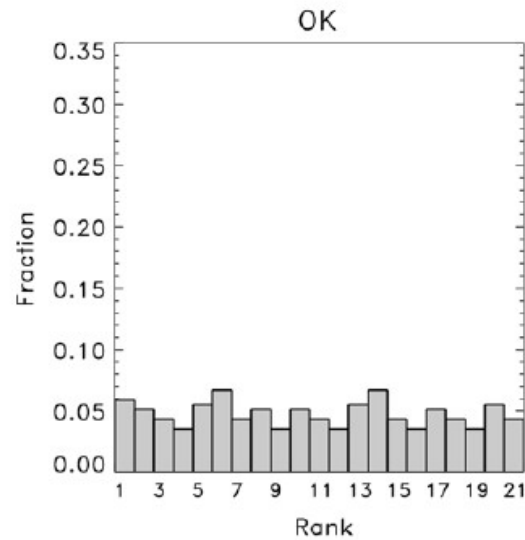
*Parent Domain (d01): 30-km*

*Inner Domain (d02): 10-km*

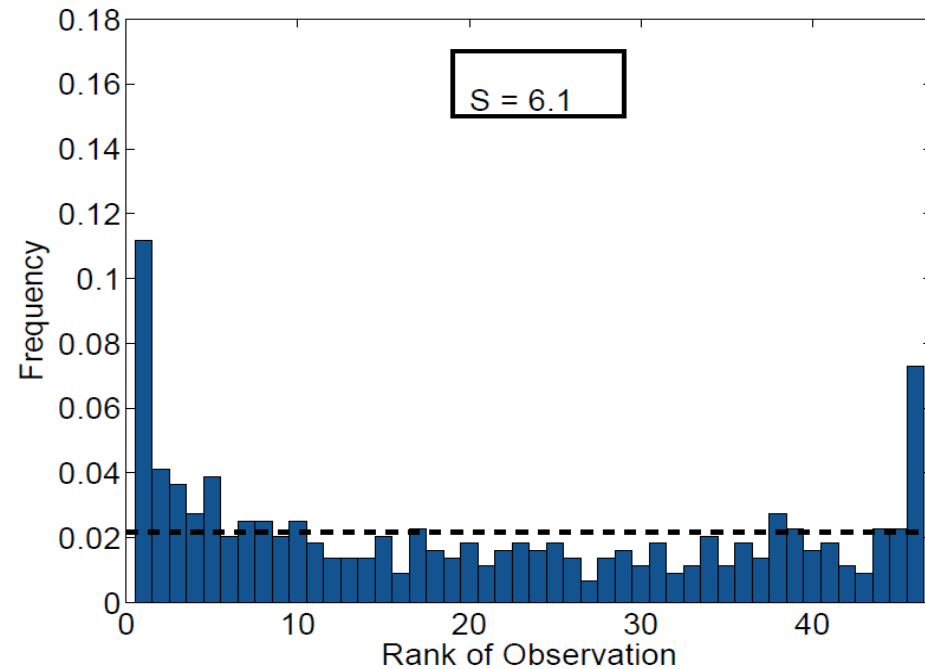
- Re-initialization every five days.
- A multi-physics and multi-analysis ensemble will be used instead of a randomly perturbed ensemble.
- The multi-physics and multi-analysis configurations allows us to select different model configurations for multiple atmospheric inversions.

*from Diaz-Isaac et al. (in prep.)*

# Rank Histograms & Score



If the ensemble is under-dispersive  
*Then the score will be greater than 1*



How to improve the score of the ensemble,  
i.e. increase the dispersion?

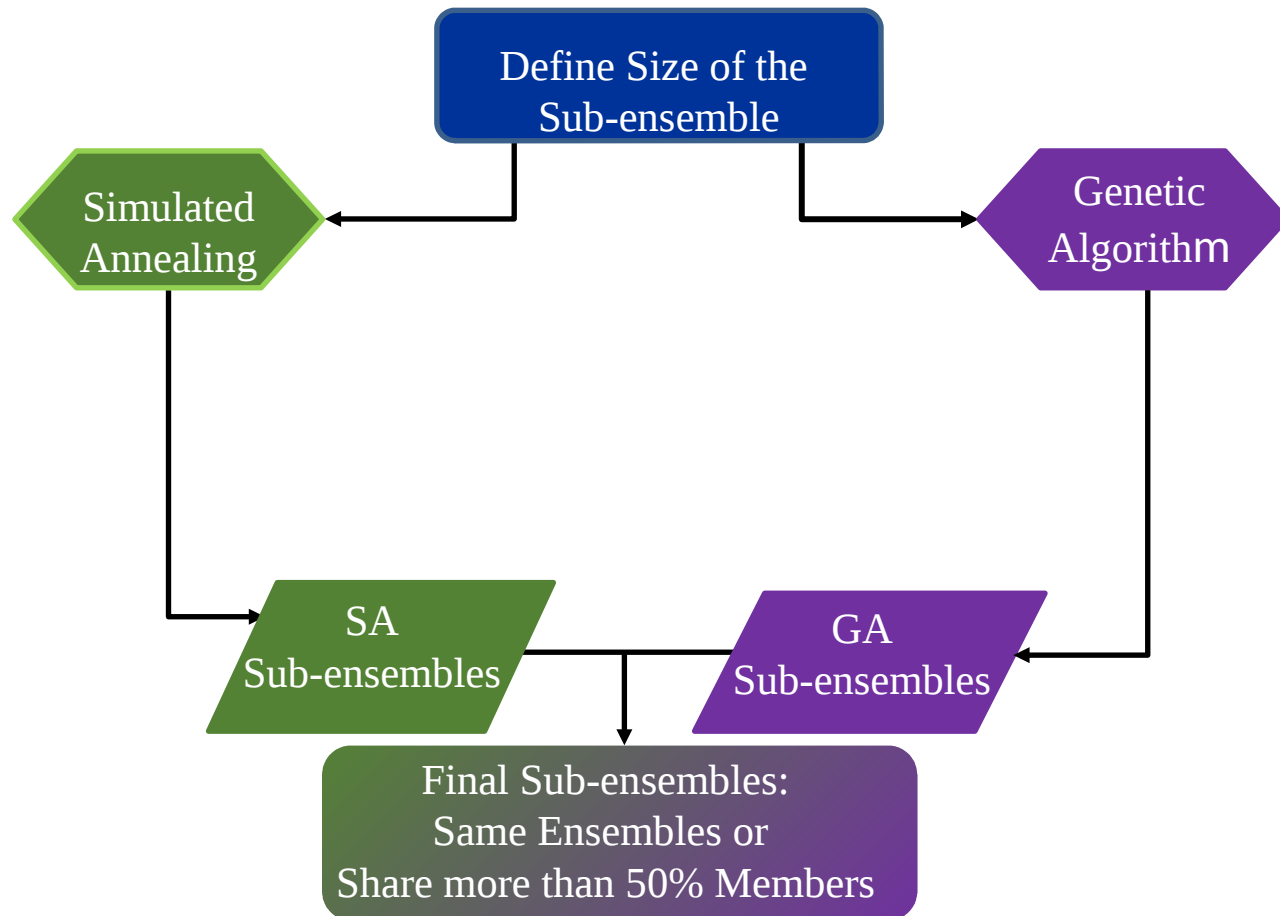
# Calibration of the ensemble

## Optimization

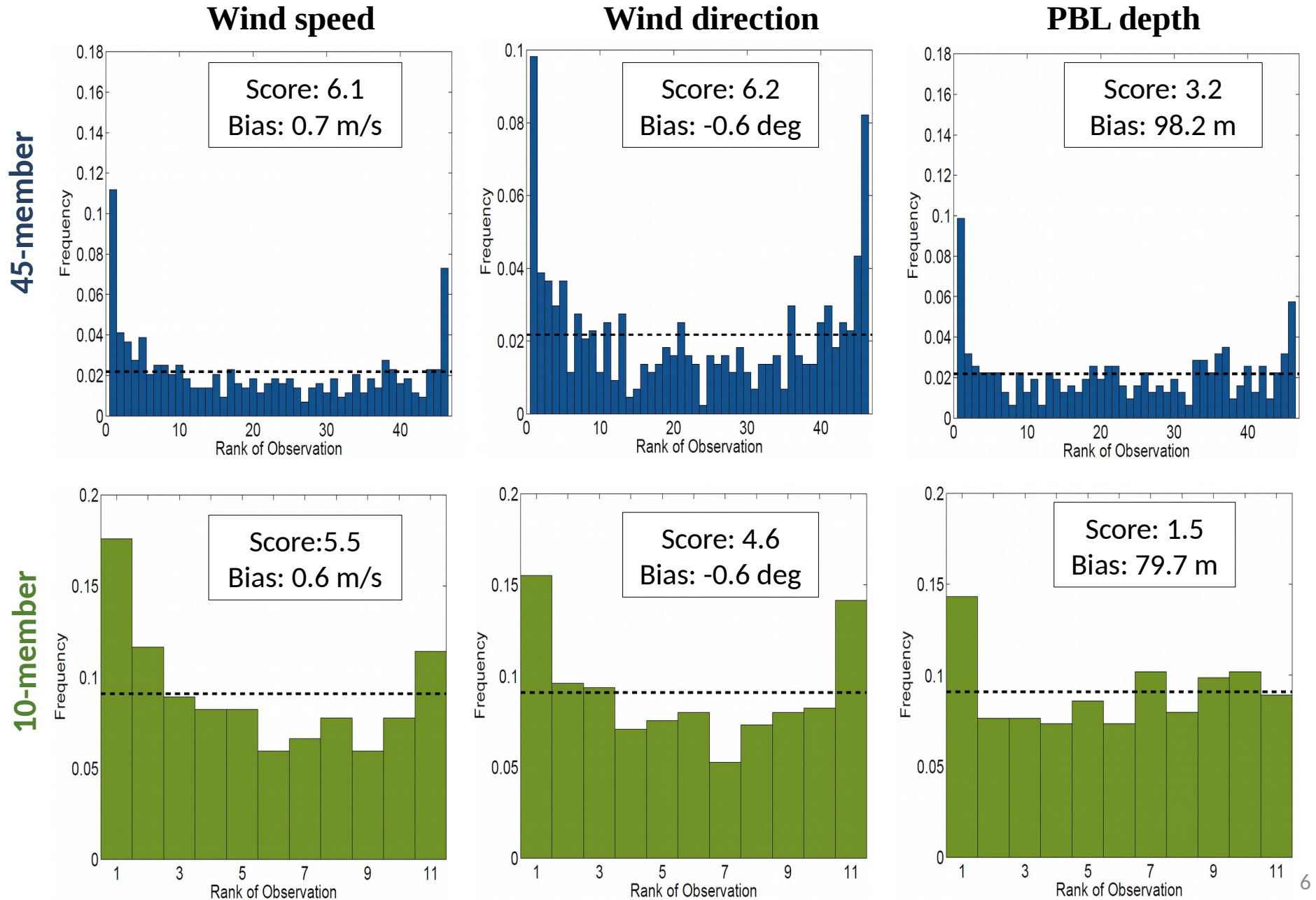
Simulated Annealing &  
Genetic Algorithm

$$S = (S_{wsp})^2 + (S_{wdi})^2 + (S_{pbl})^2$$

*An automatic selection of a sub-ensemble is used to minimize the score.*



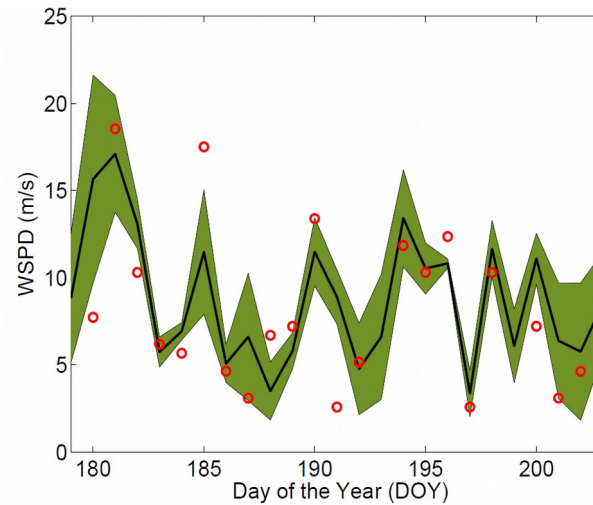
# Simulated Annealing 10-member Sub-Ensemble



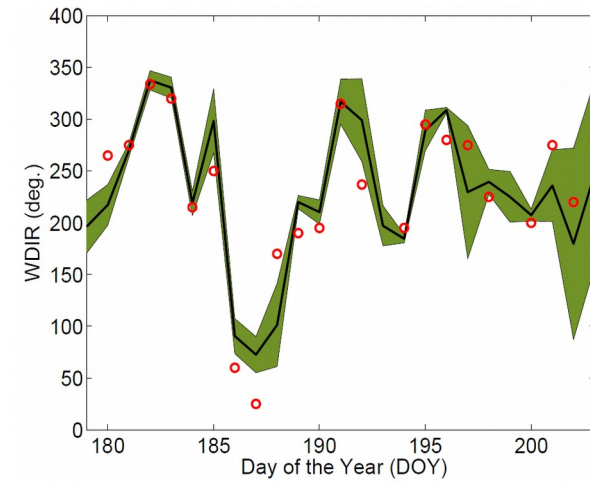
from Diaz-Isaac et al. (in prep.)

# Ensemble-based CO<sub>2</sub> Variance

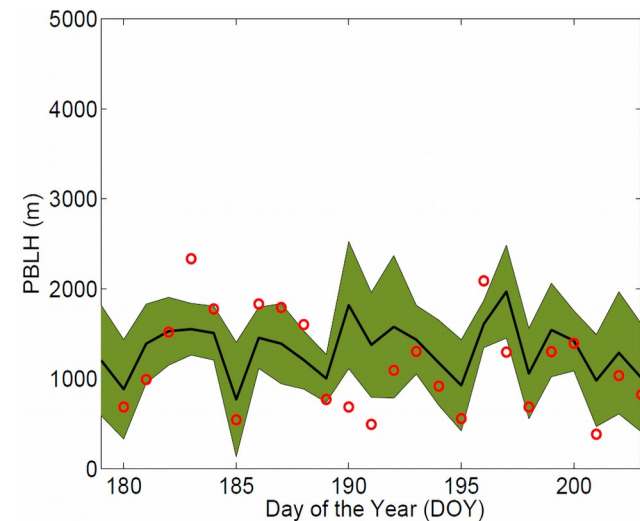
## Wind Speed at DVN



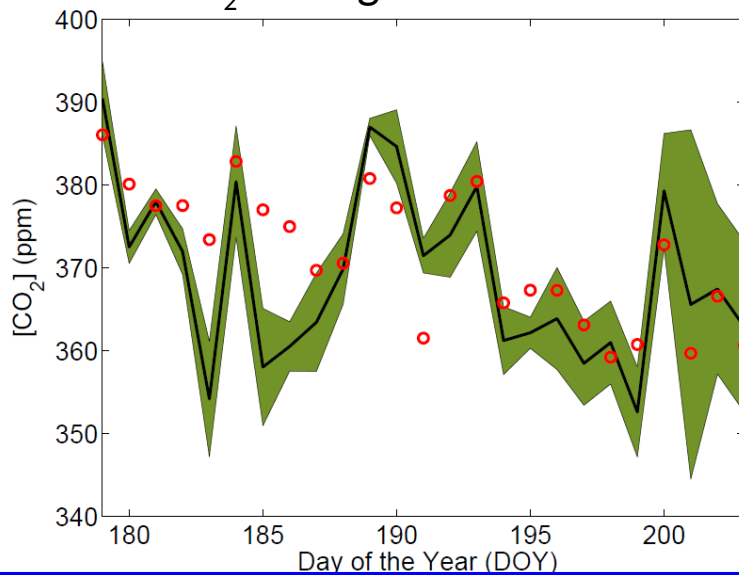
## Wind Direction at DVN



## PBL Height at DVN



## CO<sub>2</sub> Mixing Ratio at WBI



*from Diaz-Isaac et al. (in prep.)*

# **Quantify transport errors in CO<sub>2</sub> mixing ratios with a small-size ensemble**

## **2. Remove the sampling noise due to the limited number of members**

*Work based on recent developments in NWP for noise filtering using an objective filter*

**Sub-question: How to define the reference (best ensemble)?**

Note: 45-member ensemble is not calibrated

# Quantify transport errors in CO2 mixing ratios with a small-size ensemble

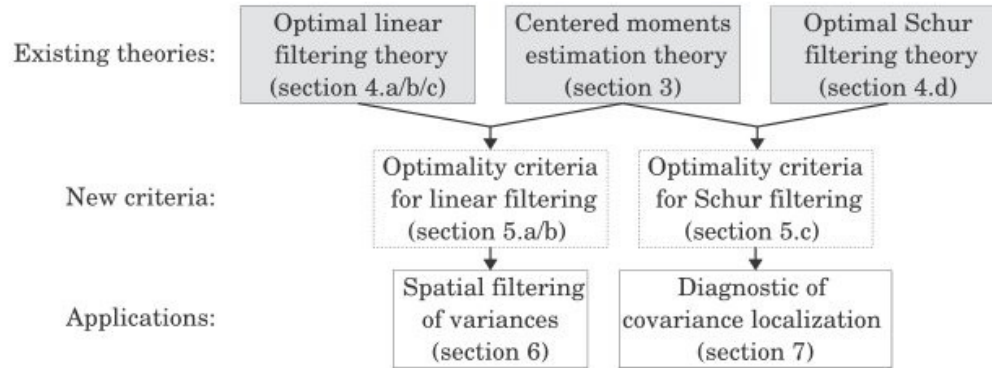


FIG. 1. Outline of the paper, from original theories to applications, via new optimality criteria definition.

## Non-Gaussian

## Gaussian

### Variance (filter)

$$\mathfrak{C}_i = \mathbb{E}[\tilde{v}_i^2] - \frac{N(N-2)(N-3)}{(N-1)(N^2-3N+3)} \mathbb{E}[\tilde{v}_i \hat{v}_i] - \frac{N^2}{(N-1)(N^2-3N+3)} \mathbb{E}[\tilde{\xi}_i],$$

$$\mathfrak{C}_i^G = \mathbb{E}[\tilde{v}_i^2] - \frac{N+1}{N-1} \mathbb{E}[\tilde{v}_i \hat{v}_i].$$

### Covariance (schur product)

$$L_{ij} = \frac{(N-1)^2}{N(N-3)} - \frac{N}{(N-2)(N-3)} \frac{\mathbb{E}[\tilde{\Xi}_{ijij}]}{\mathbb{E}[\tilde{B}_{ij}^2]} + \frac{N-1}{N(N-2)(N-3)} \frac{\mathbb{E}[\tilde{v}_i \tilde{v}_j]}{\mathbb{E}[\tilde{B}_{ij}^2]}.$$

$$\mathfrak{C}_i = \mathbb{E}[\tilde{v}_i^2] - \frac{N(N-2)(N-3)}{(N-1)(N^2-3N+3)} \mathbb{E}[\tilde{v}_i \hat{v}_i] - \frac{N^2}{(N-1)(N^2-3N+3)} \mathbb{E}[\tilde{\xi}_i],$$

# Impact of the calibration on Filtered CO<sub>2</sub> Variances and Covariances using **calibrated and random ensembles of 5 and 8members**

Monthly averages of the filtered hourly  
results

27 June to 20 July, 2008

## 1. “Random ensembles” were generated with randomly selected members

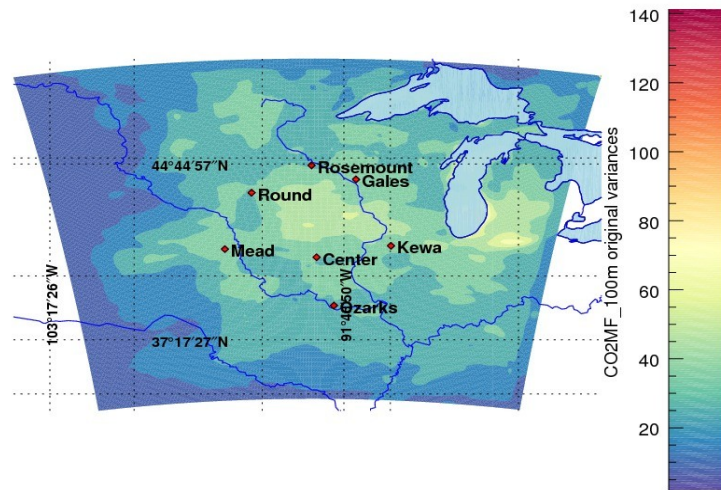
- *Random ensembles (“random X-member”) do not share any members with calibrated ensembles (“calibrated X-member”) = members never selected by calibration procedure*
- *Random ensembles of different sizes (i.e. 5-member and 8-member) share only one member (I didn't do that on purpose, it just turned out to be that way)*

## 2. “Calibrated ensembles” were generated with two methods:

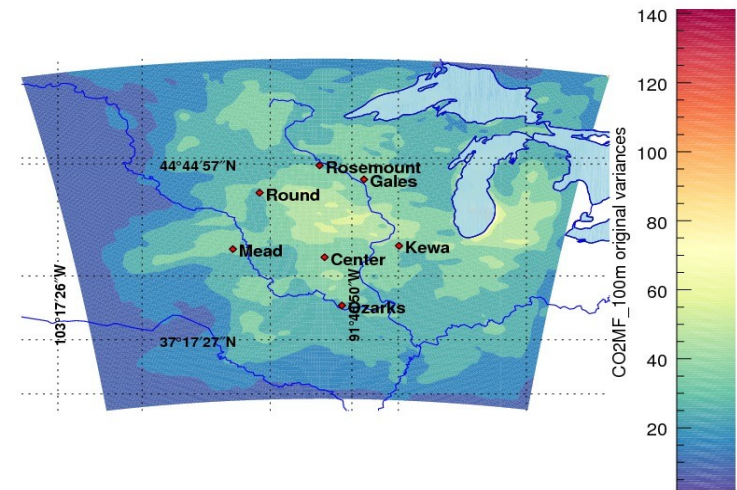
- *Simulated Annealing (SA): best option AND best option most similar to GA*
- *Genetic Algorithm (GA): best option AND best option most similar to SA*

*Note: before, I was only using “SA ensembles most similar to GA” (and not “best option”)*

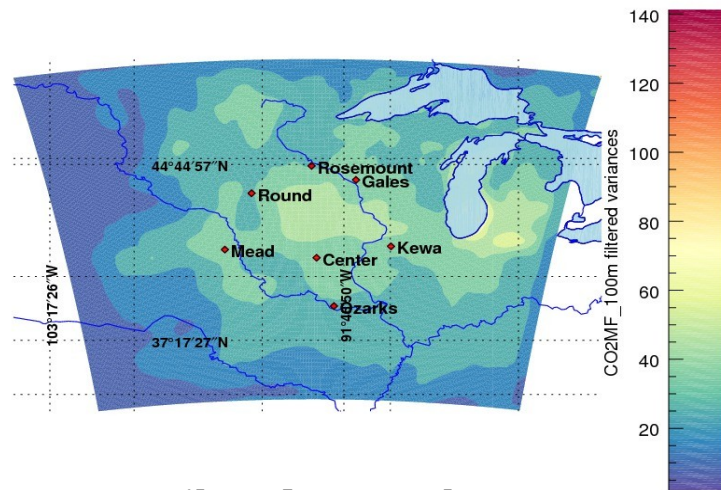
# Quantify transport errors in CO<sub>2</sub> mixing ratios with a small-size ensemble



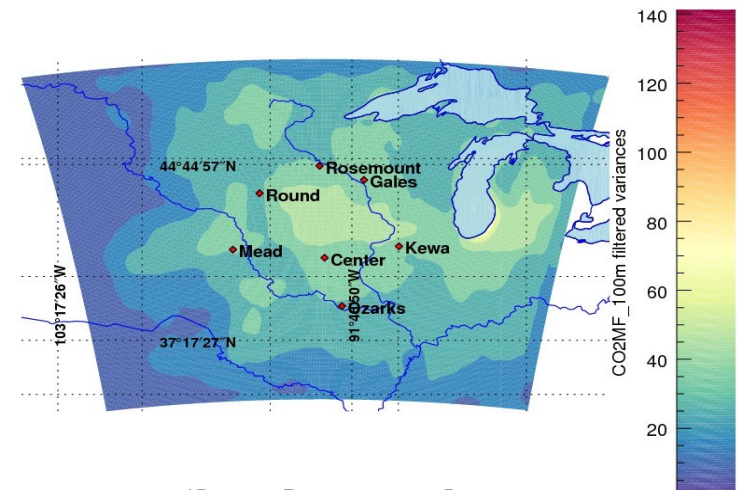
*Raw 45 members*



*Raw 25 members*



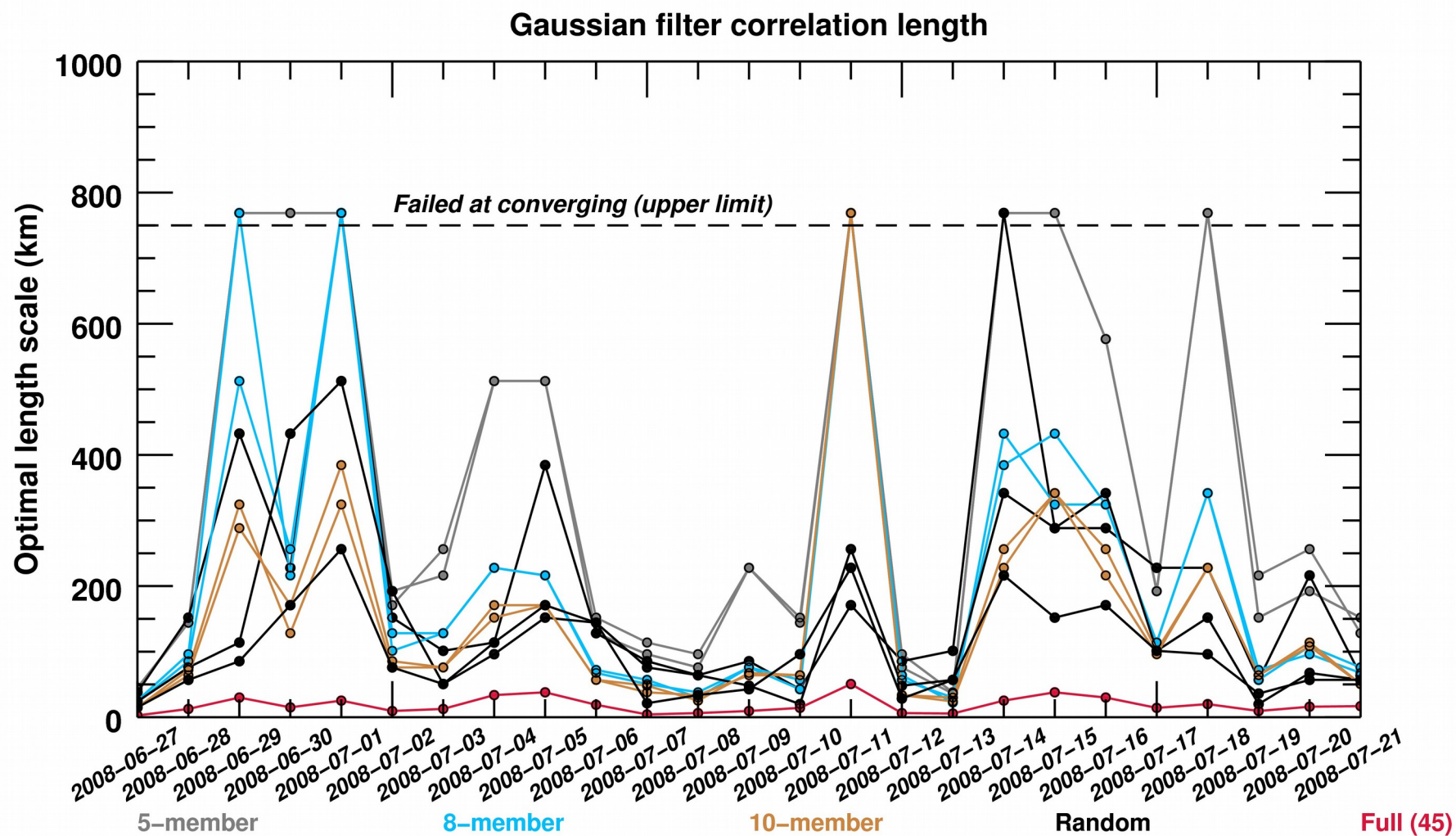
*Filtered 45 members*

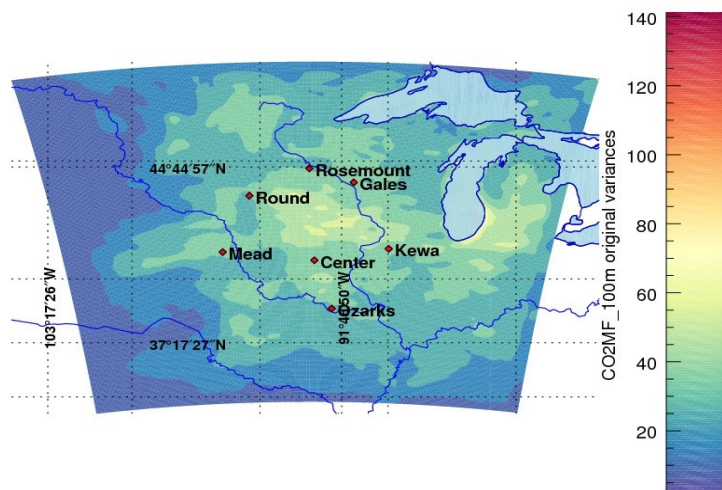


*Filtered 25 members*

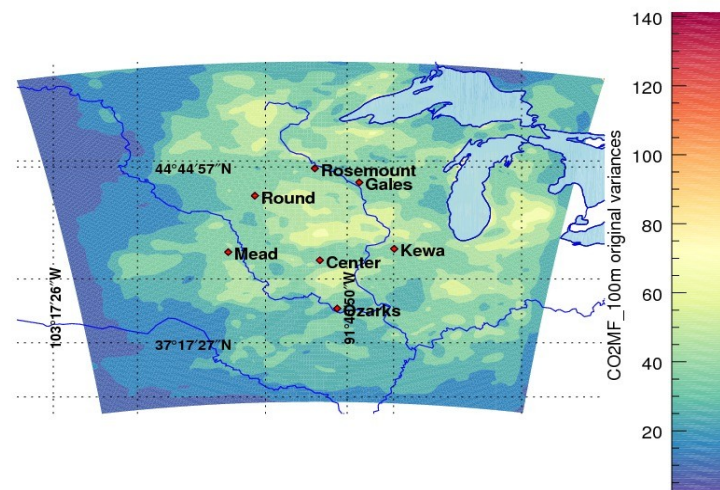
Optimal sub-ensemble = sufficient number of members (here 25 members) and calibration of the ensemble

# Convergence of the filter for variances

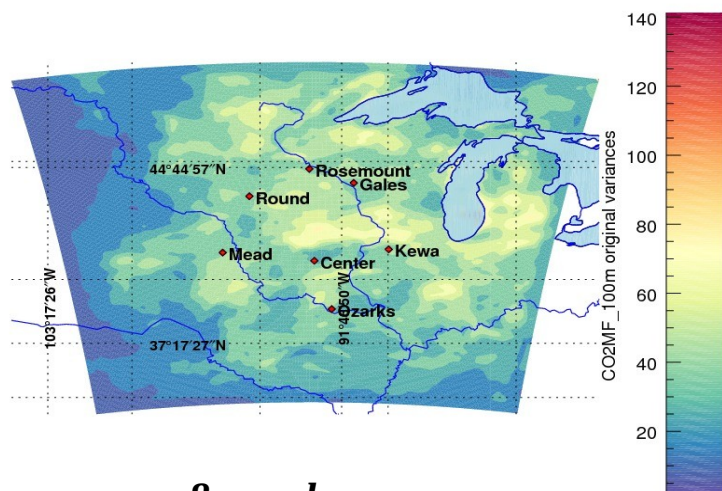




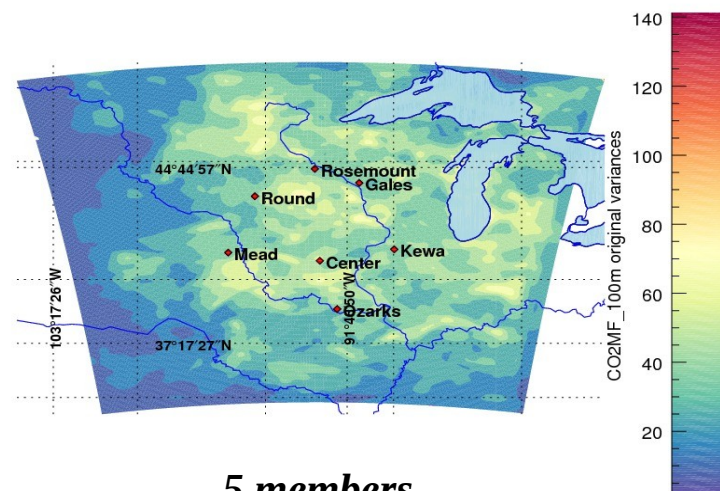
*25 members*



*10 members*

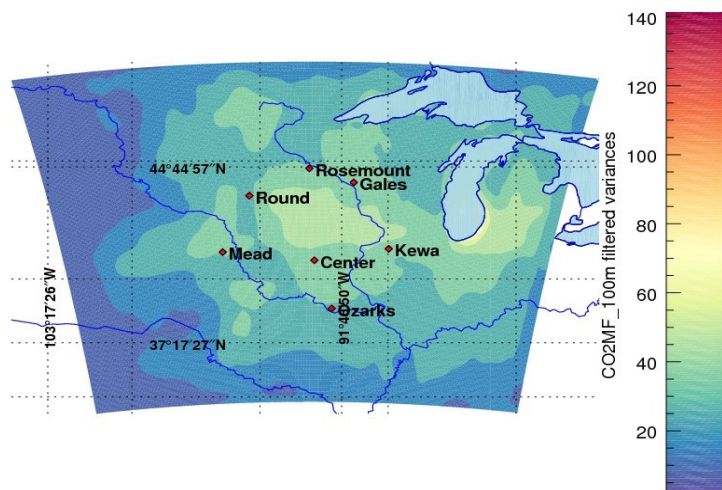


*8 members*

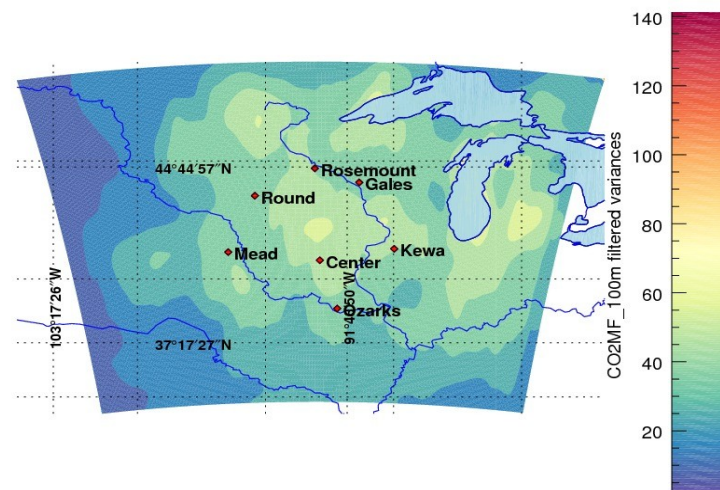


*5 members*

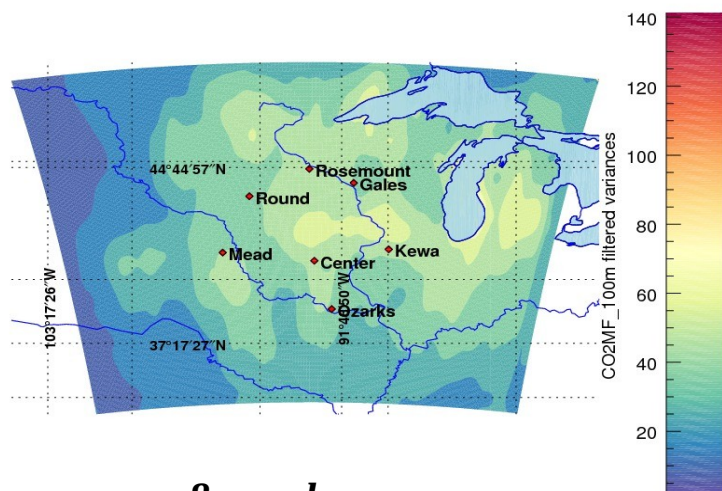
Unfiltered variances averaged over one month (in ppm<sup>2</sup>)



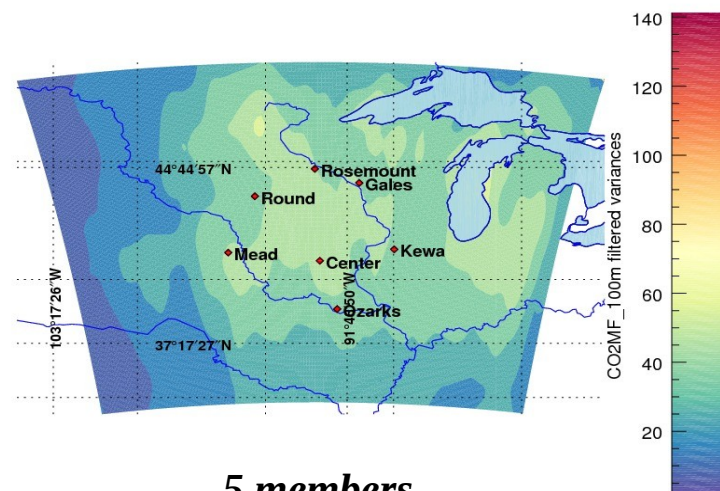
*25 members*



*10 members*



*8 members*



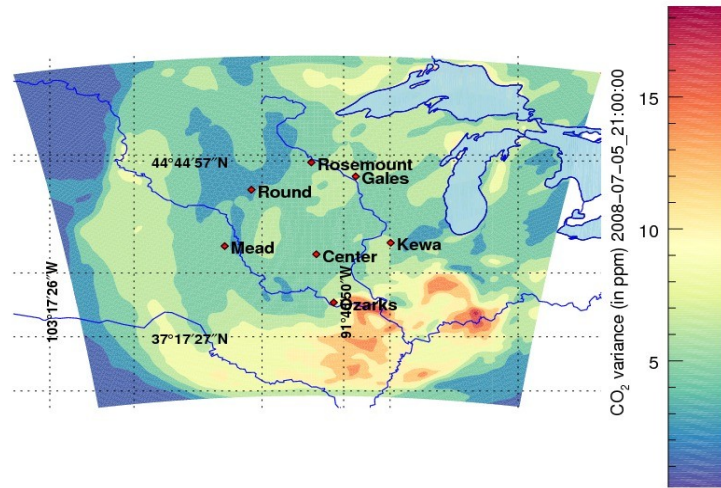
*5 members*

**Filtered** variances averaged over one month (in ppm<sup>2</sup>)

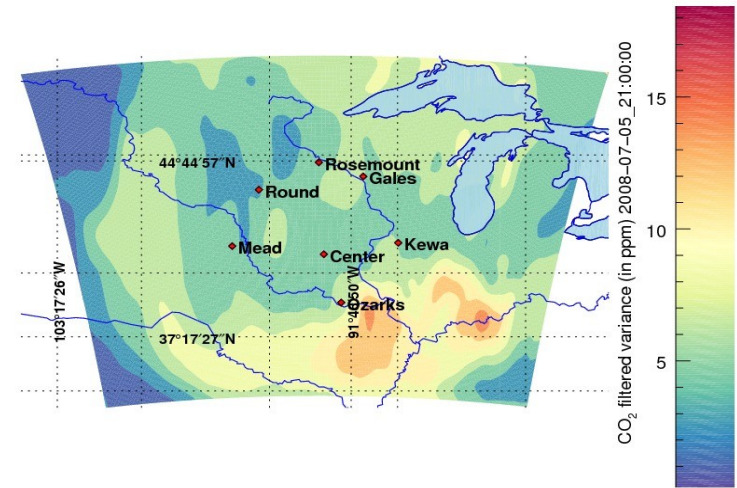
## **An example**

I show here an example of hourly variances for July 5 and July 20 of 2008

5 July

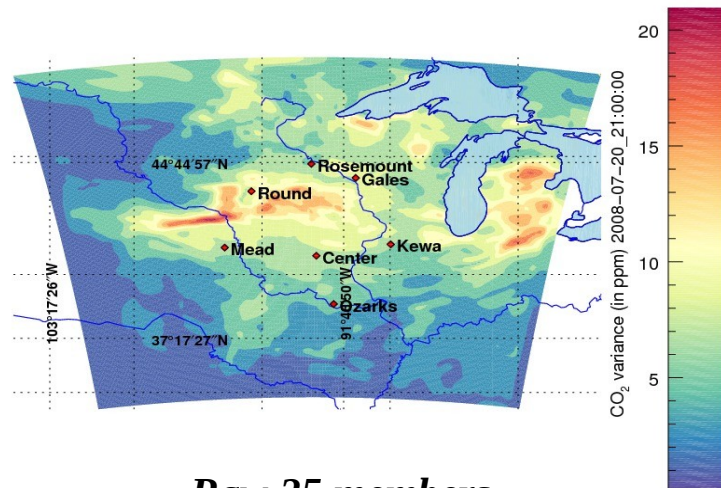


*Raw 25 members*

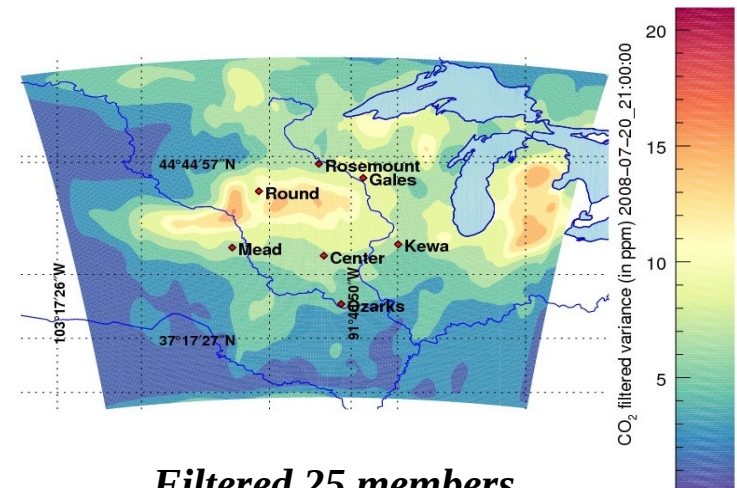


*Filtered 25 members*

20 July



*Raw 25 members*



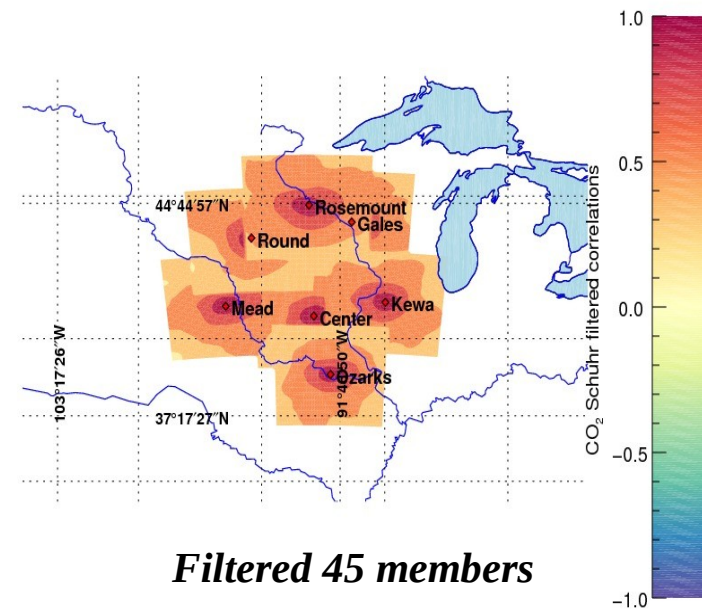
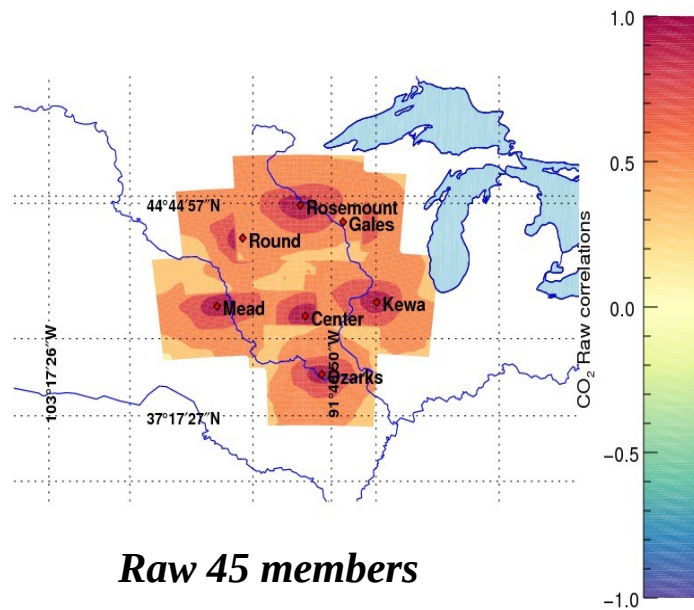
*Filtered 25 members*

25-member variances averaged over one month (in ppm<sup>2</sup>)

### **And the error covariances**

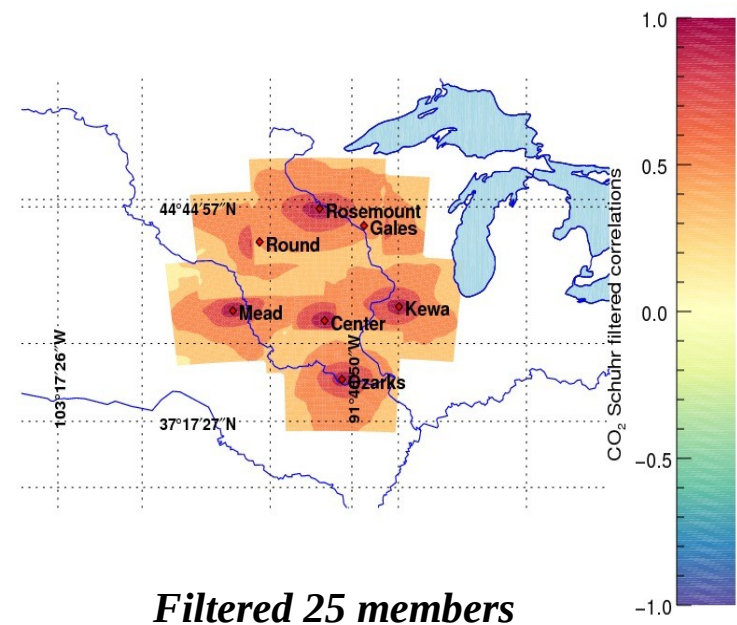
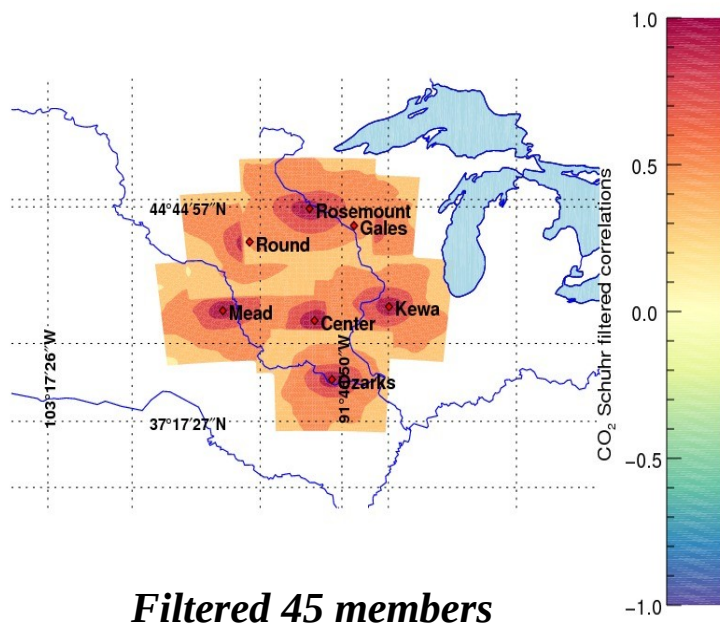
Here is the monthly averaged error correlations after using Menetrier's filter (Schur product here)

# Filtering covariances (Schur product) of calibrated ensembles



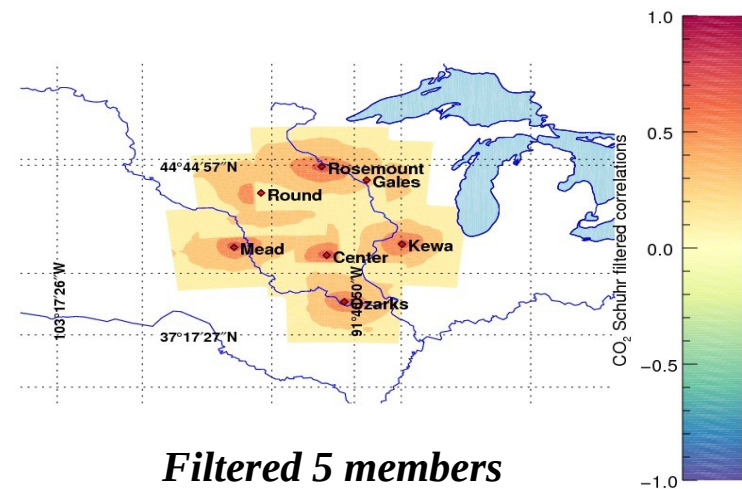
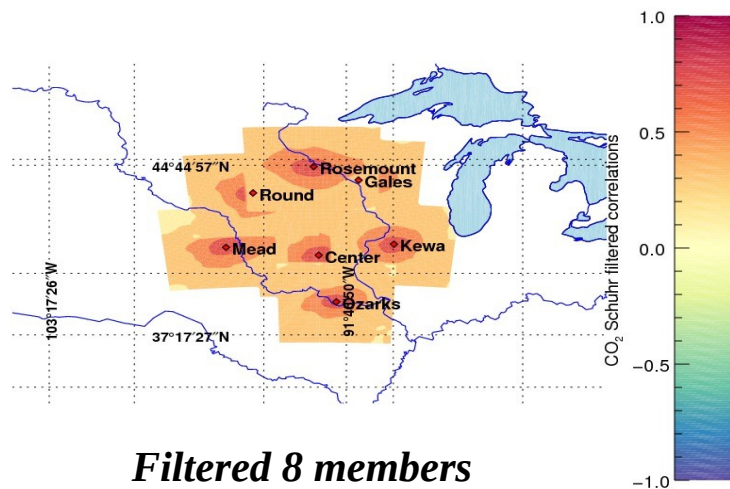
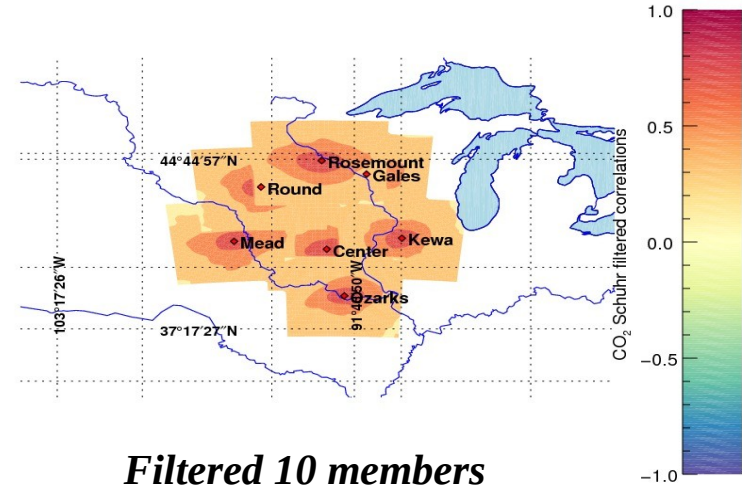
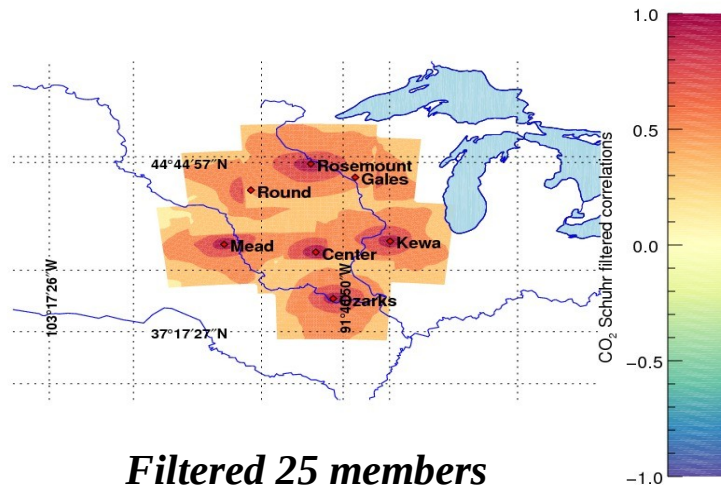
Full (=45-member) ensemble error correlations averaged over one month

## Filtering covariances (Schur product) of calibrated ensembles



**Full (=45) and 25-member** error correlations averaged over one month

# Filtering covariances (Schur product) of calibrated ensembles



# Conclusions and Perspectives

## **1. Generate a calibrated ensemble which represents the characteristics of transport errors using a minimum number of members**

*Starting from 45 members, small-size ensembles of 8 and 10 members are able to represent the observed CO<sub>2</sub> variances*

*Initial dispersion was small which limits our ability to match exactly the model errors*

→ ***Generate perturbed ensembles to increase the dispersion***

## **2. Remove the sampling noise due to the limited number of members**

Calibrated sub-ensembles show specific error structures not visible in the original ensemble and in random sub-ensembles

→ Need to create error covariance matrices for the CO<sub>2</sub> atmospheric inversion