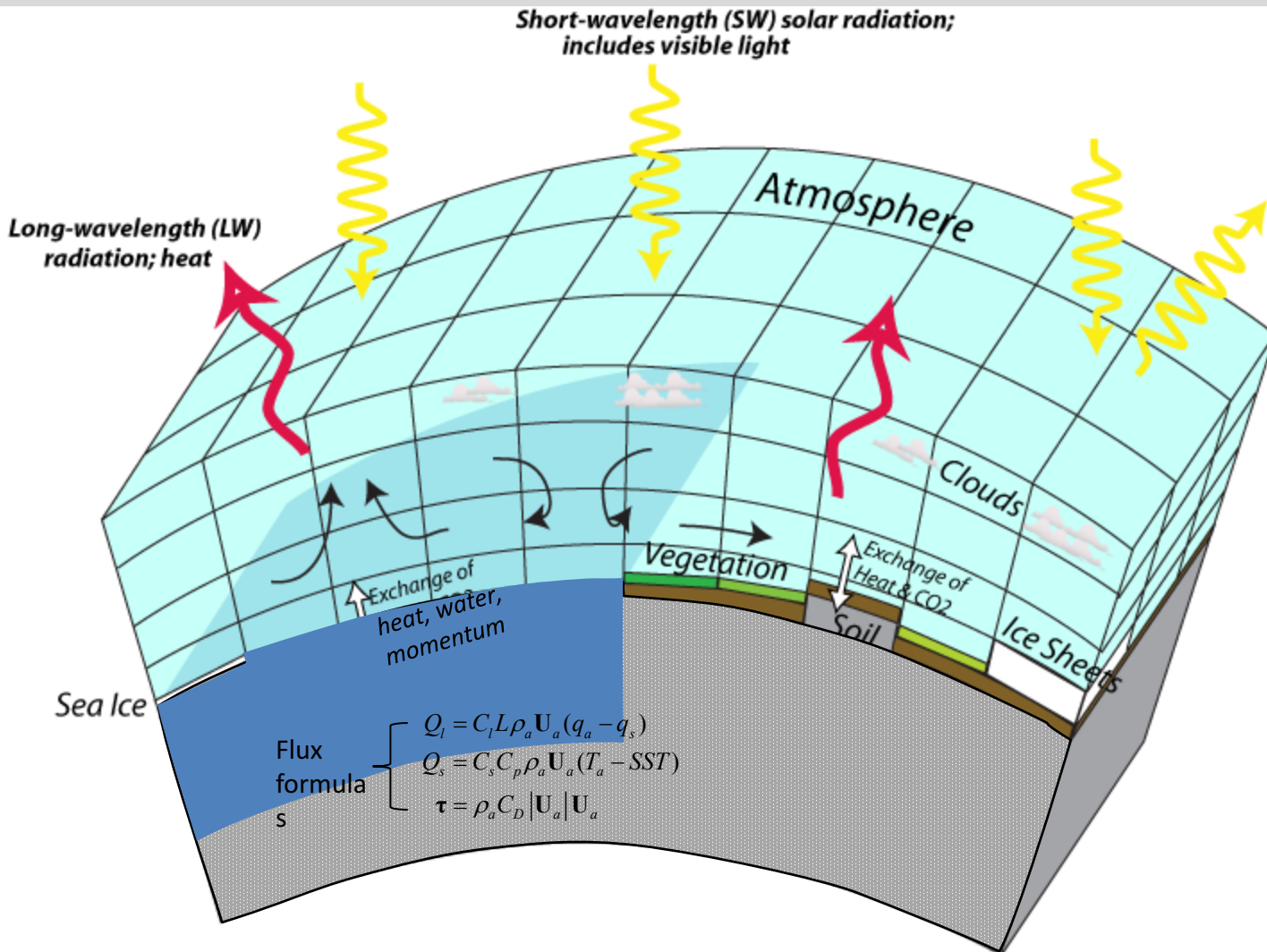


An incremental approach to fixing surface fluxes

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L. Chen, S. Grodsky



Surface heat/water fluxes are the residual of the atmospheric heat/freshwater budgets!



Different reanalyses have mean estimates that differ by 10-30Wm⁻²!

How to reduce HF errors

Meteorological approach:

Fix each component *a posteriori*:

Large and Yeager (2009); Brodeau et al. (2010)

Parameter estimation:

Kang and Kalnay (2013); Bateni and Entekhabi (2012)

Oceanographic approach:

Profiles as a constraint:

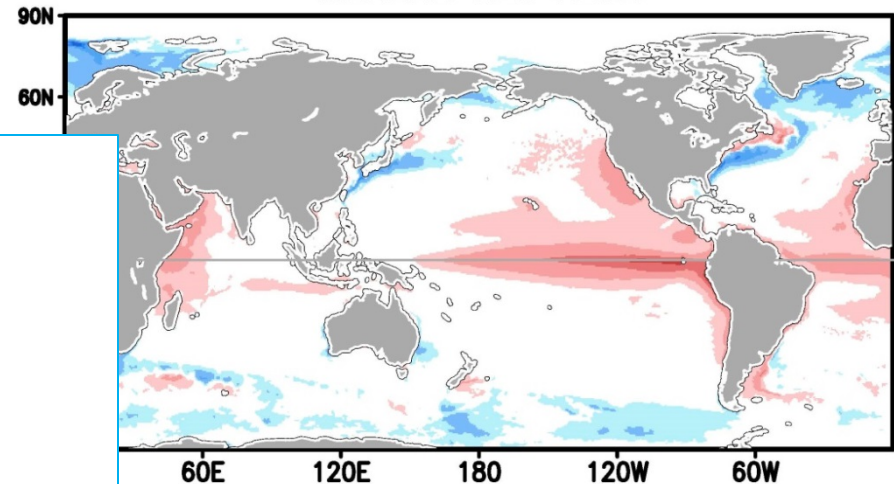
0) *DaSilva (1994); Lamb (1981); Hastenrath & Merle (1983)*

1) *Isemer et al. (1989); Grist & Josey (2003)*

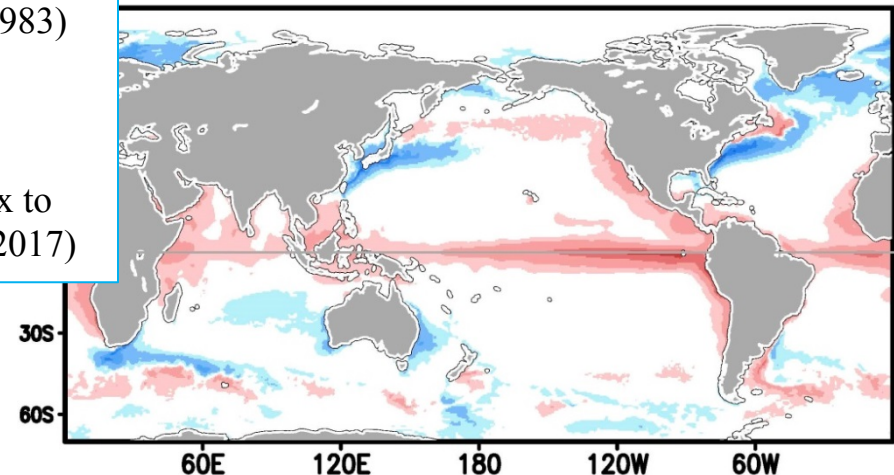
2) *Stammer et al. (2004)*

(there is a related issue of trying to adjust momentum flux to balance horizontal pressure gradients, e.g. *Waters et al., 2017*)

MERRA2 NET FLUX



ERA-I NET FLUX



SODA3

Ocean/ice Model

- MOM v5.1, tripolar $0.25^\circ \times 0.25^\circ \times 50$ lev
- SIS 5 layer sea ice
- Coastal tide & internal tide mixing
- *Dai and et al.* rivers, *Bamber et al.* Greenland
- Restoring of temperature and salinity (WOA13) below 2 km depth.
- Multiple forcings

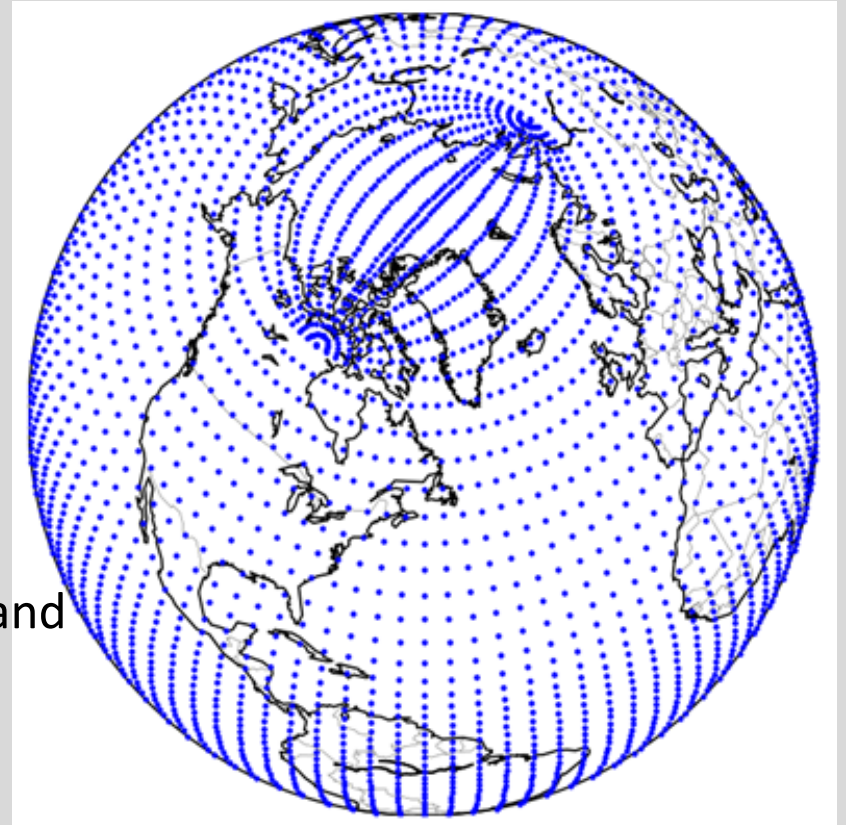
Data Assimilation

- Ol-like sequential assimilation $\omega^a = \omega^f + \mathbf{K}[\omega^o - \mathbf{H}(\omega^f)]$
- Data: WDB13 profiles, SST (ICOADS2.5, PATHFINDER AVHRR, VIIRS/MODIS)
- We also have a 'static' LETKF

Bias Correction

- Surface flux bias correction based on examination of analysis increments:

$$\mathbf{K}[\omega^o - \mathbf{H}(\omega^f)]$$



Ongoing SODA3 experiments*

(1980-2016)

Name	Forcing	Bulk Formula	Fluxes modified?	Completed?
Soda3.3.1	MERRA2	Large & Yeager	no	yes
Soda3.3.2	MERRA2	COARE4 (& 10% speedup of u10m)	yes	Just started
Soda3.4.1	ERA-Int	Large & Yeager	no	yes
Soda3.4.2	ERA-Int	COARE4	yes	mostly
Soda3.5.2	ERA20C	COARE4	yes	no
Soda3.6.2	NOAA 20CRv2	?	yes	no
Soda3.7.1	JMA55	Large & Yeager	no	yes
Soda3.7.2	JMA55	COARE4	yes	mostly
Soda3.8.2	CORE2	Large & Yeager	no	mostly

*we're using www.soda.umd.edu as our distribution port

Liquid ocean heat budget

$$h\rho C_p \frac{\overline{D\theta}^z}{Dt} \cong Q$$

Following incremental 4DVar: approximate vertically averaged increment heat budget

$$\underbrace{h\rho C_p \frac{\overline{\delta\theta}}{\partial t}}_{\text{ocean}} + \underbrace{L\rho \frac{\partial \delta h_i}{\partial t}}_{\text{ice}} = \overline{Q^f} - Q^f$$

A formula for improving net surface heat flux:

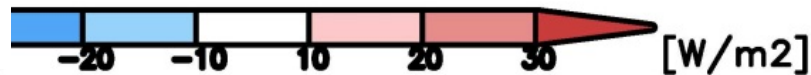
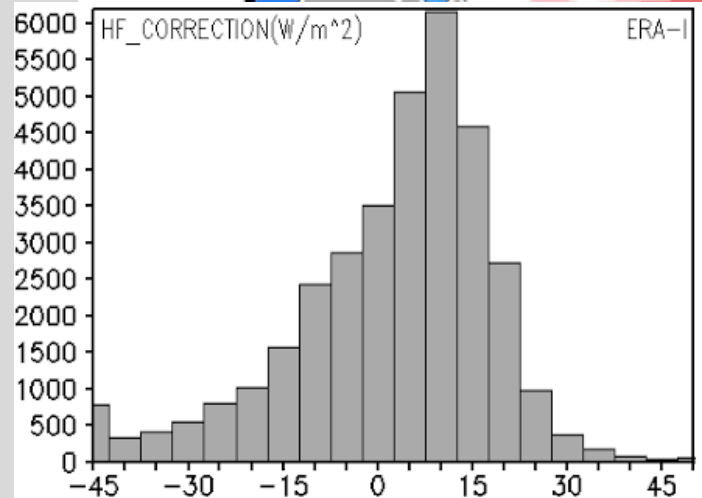
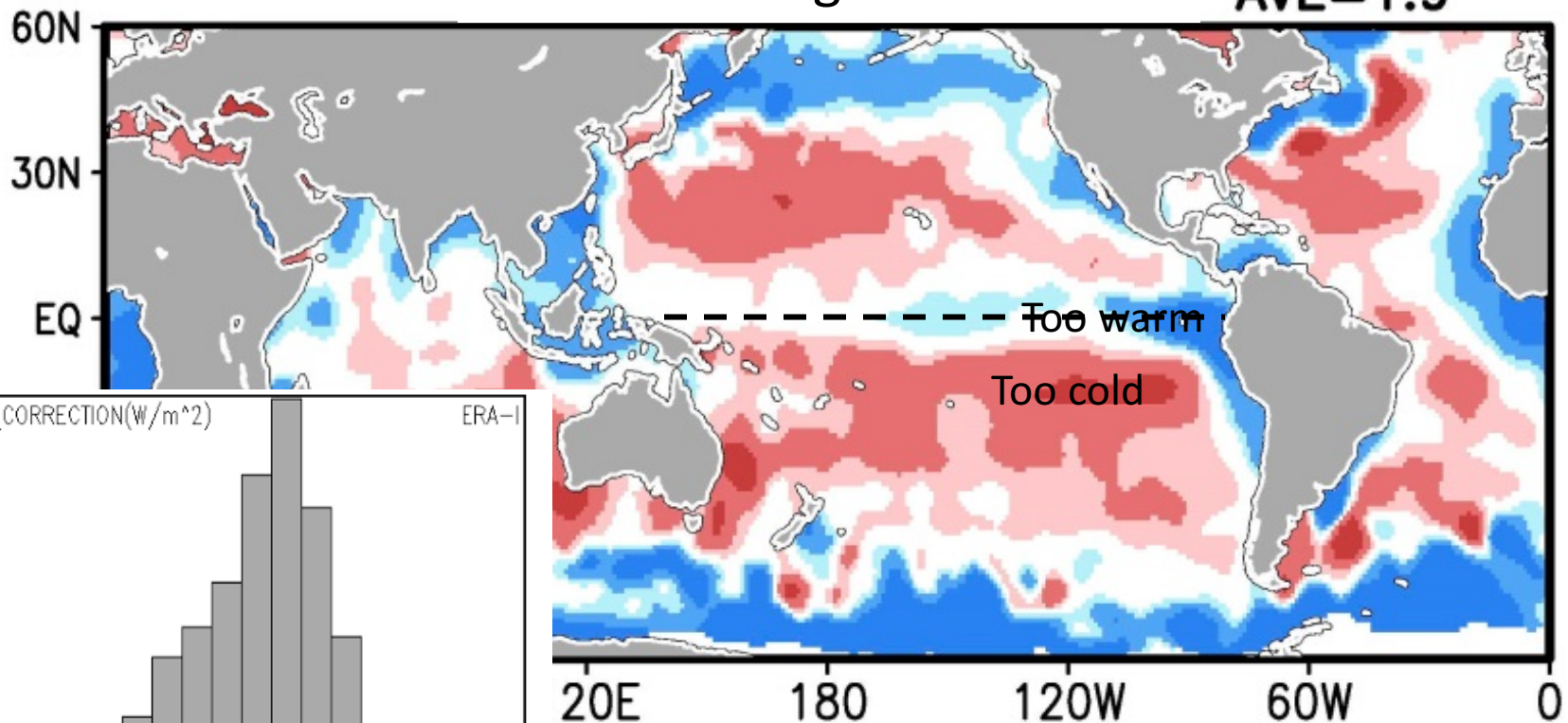
$$Q^{improved} \cong Q^f + \overline{\delta\theta} \frac{\rho C_p h}{\Delta t} + \delta h_i \frac{L\rho}{\Delta t}$$

$$\text{SODA3: } \frac{\partial}{\partial \theta} \frac{\rho C_p h}{\Delta t}$$

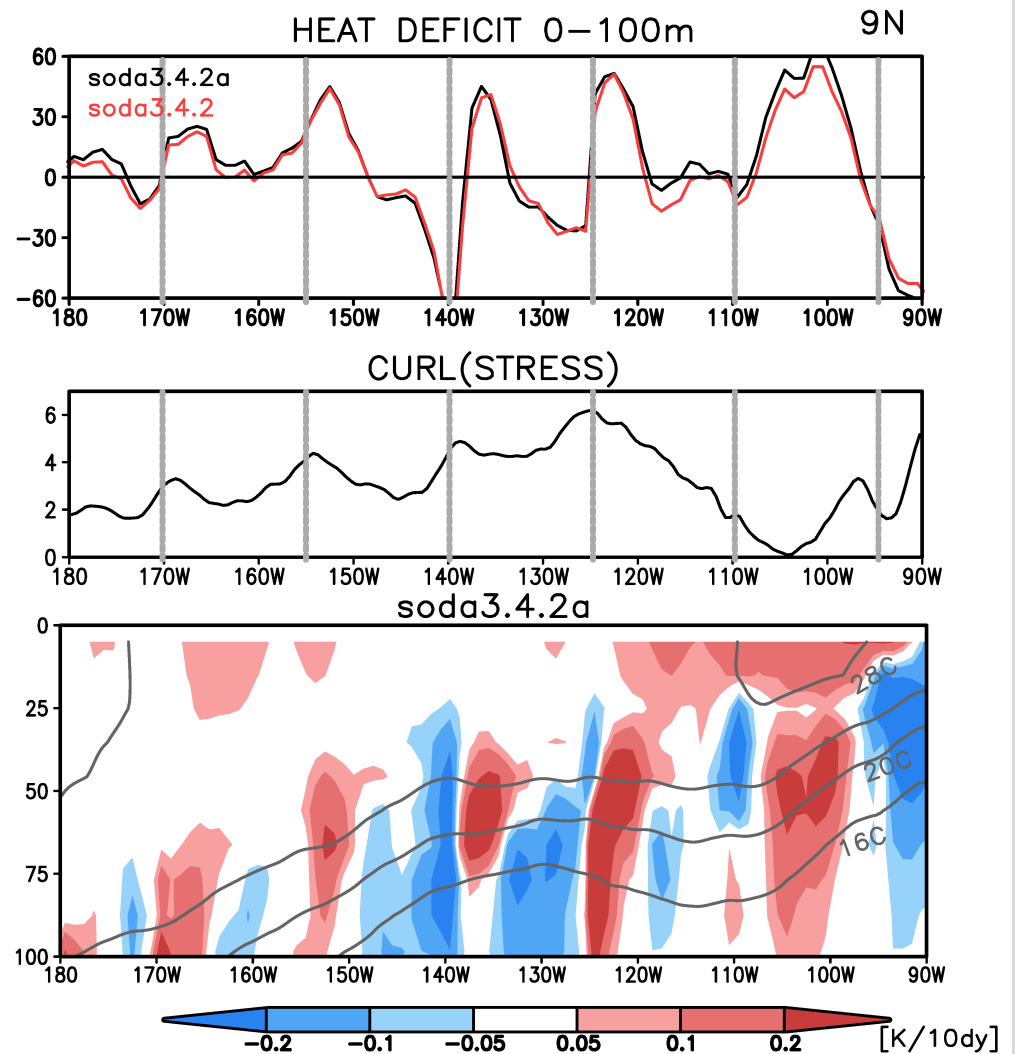
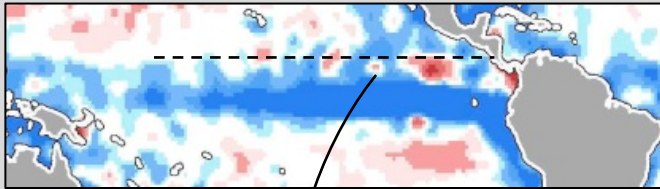
$$h = mld$$

ERA-Int forcing 2007-2014

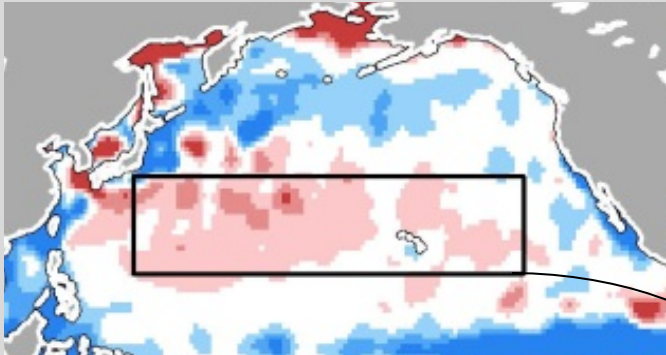
AVE=1.9



TAO/Triton moorings and $\frac{\partial}{\partial \theta} \frac{\rho C_p h}{\Delta t}$

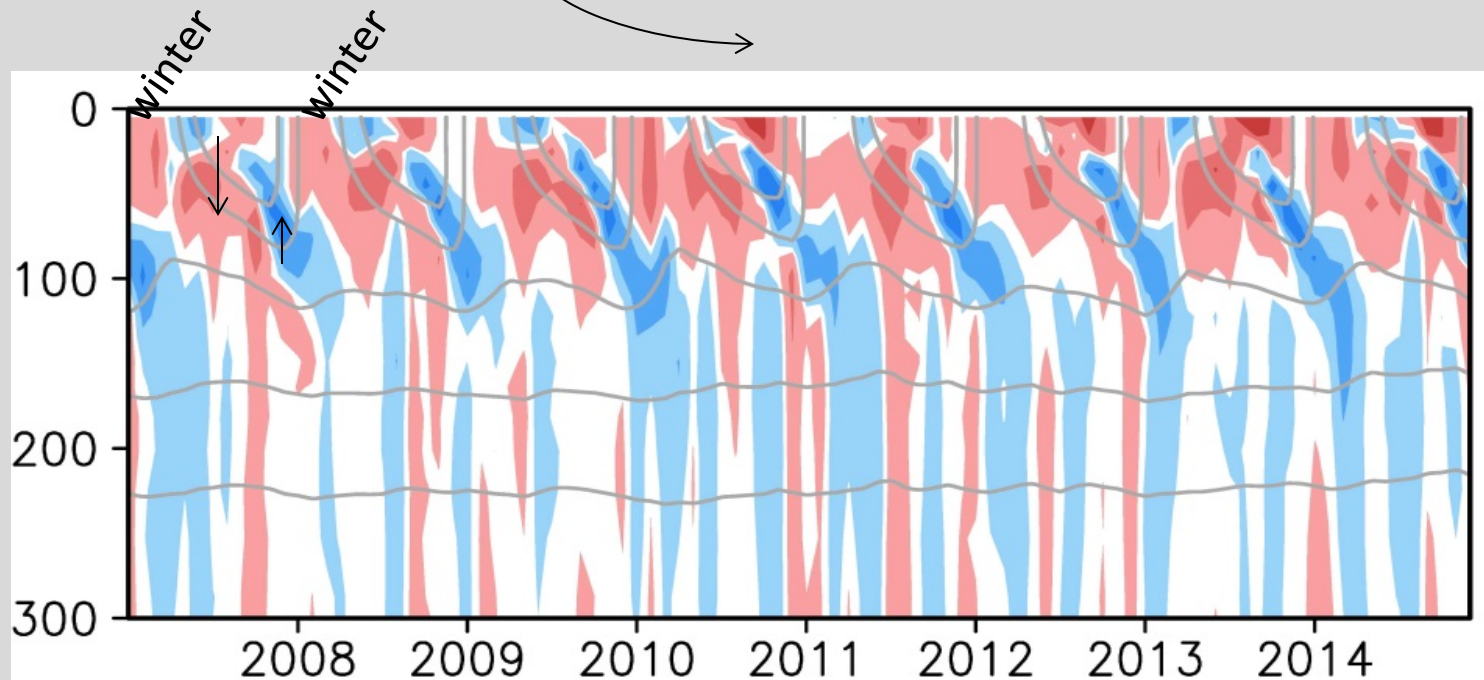


Seasonal cycle of $\delta\theta$

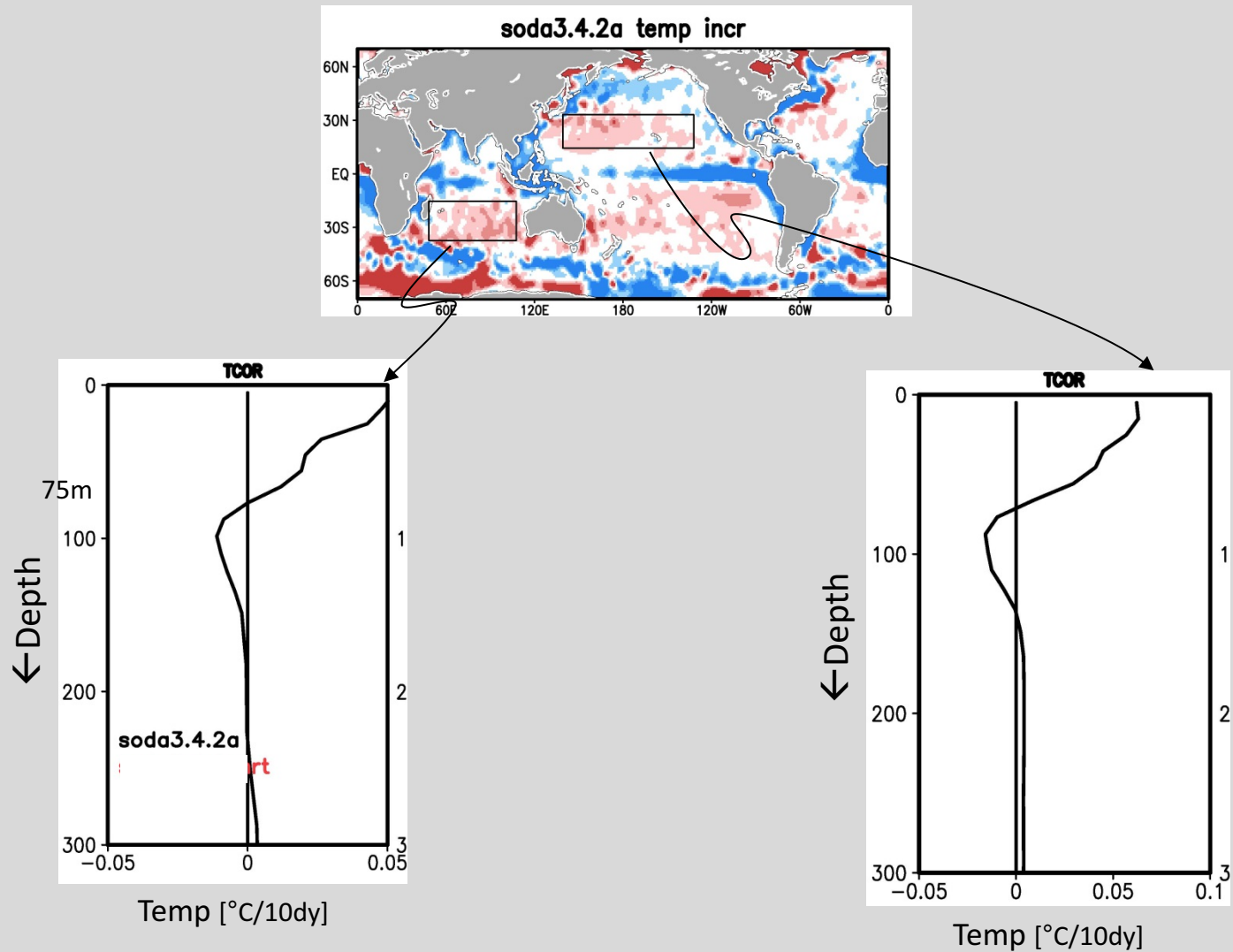


Impact of increments

- Deepens summer mixed layer,
- Weakens ΔT at the base of the winter mixed layer



Mean $\delta\theta(z)$



Modify net surface heat flux and
repeat SODA3 during 2007-2014

$$\frac{D\mathbf{u}}{Dt} = \dots$$

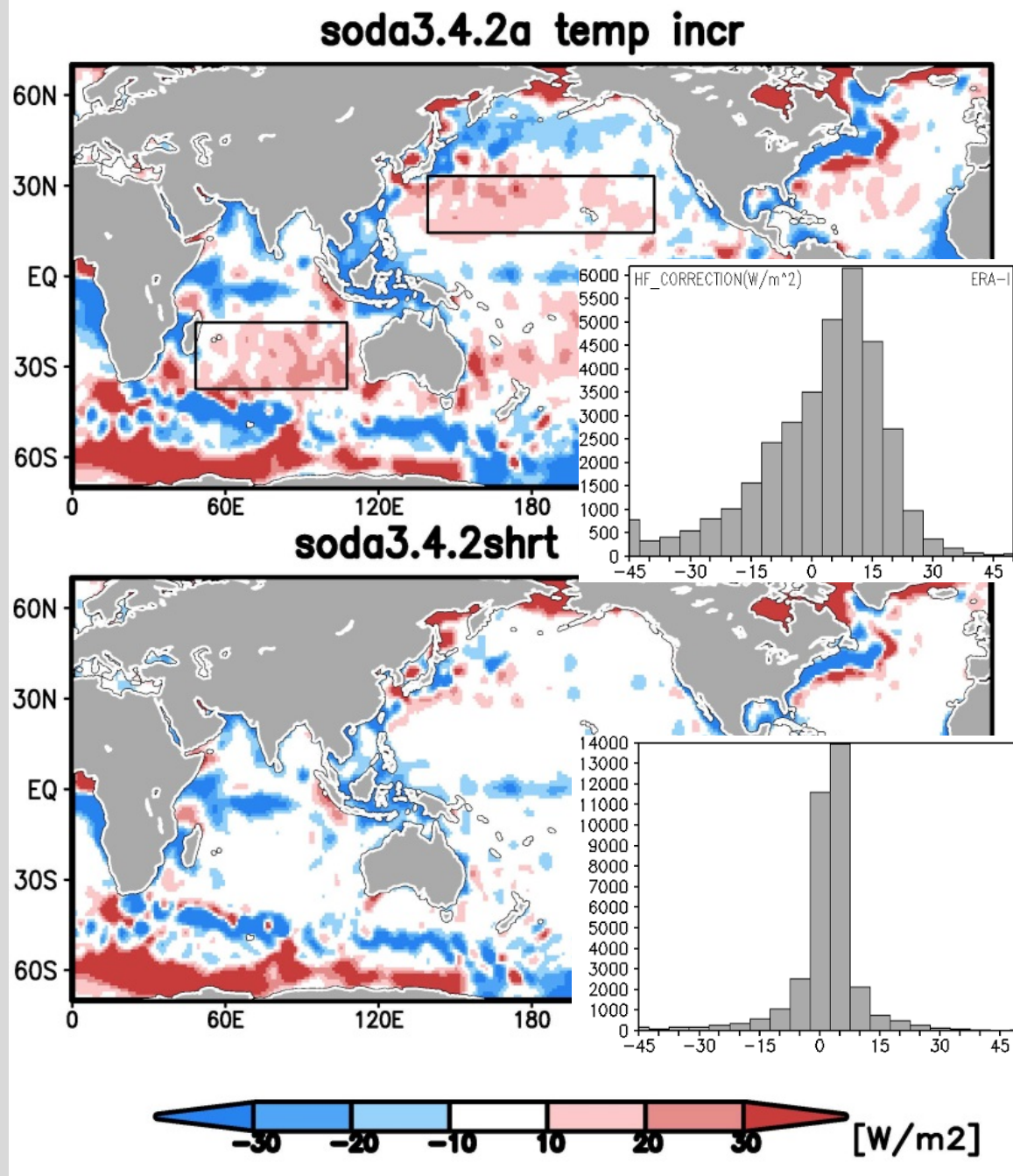
$$\frac{DS}{Dt} = \dots$$

$$\frac{D\theta}{Dt} \cong d(z) \frac{Q + \delta Q}{\rho C_p}$$

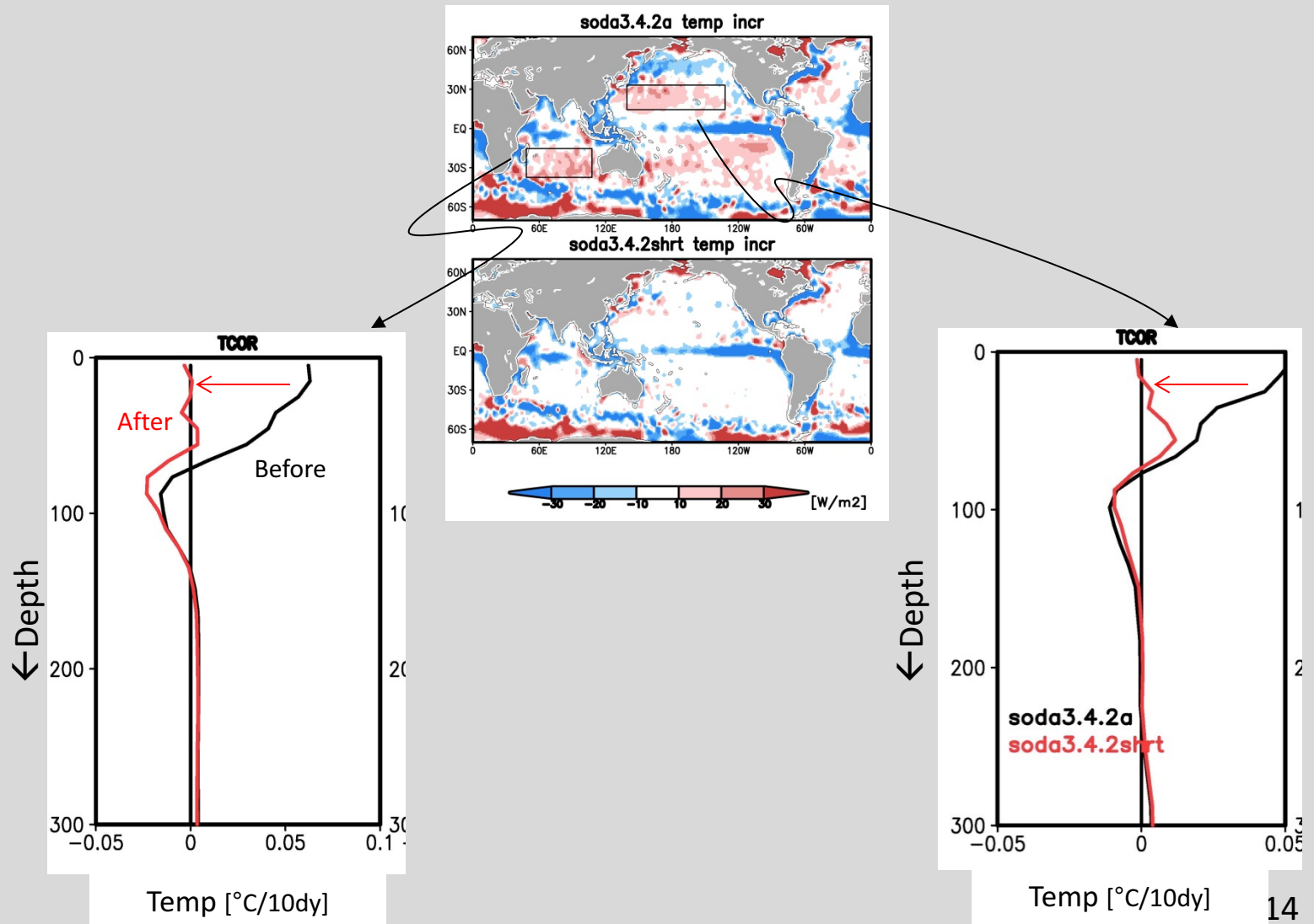
$$\frac{\partial}{\partial \theta} \frac{\rho C_p h}{\Delta t}$$

Before

After



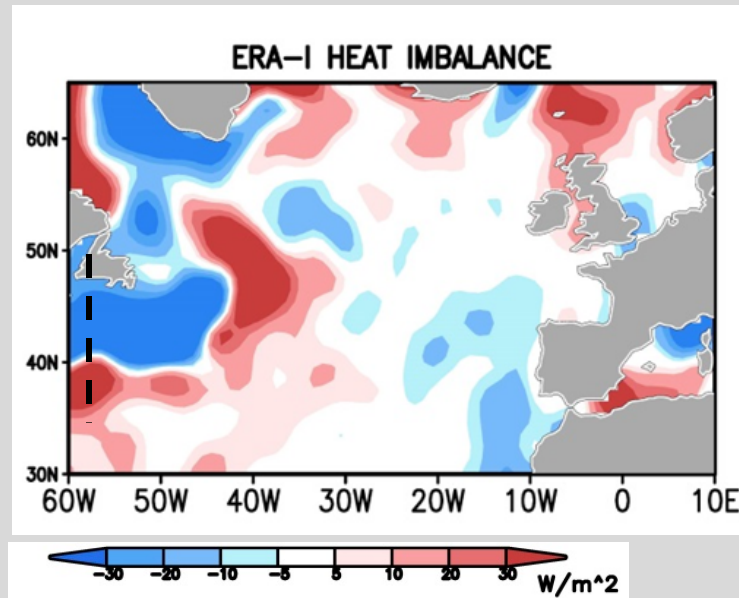
Recalculate $\delta\theta(z)$



North Atlantic $\frac{\partial}{\partial t} \frac{\rho C_p h}{\Delta t}$

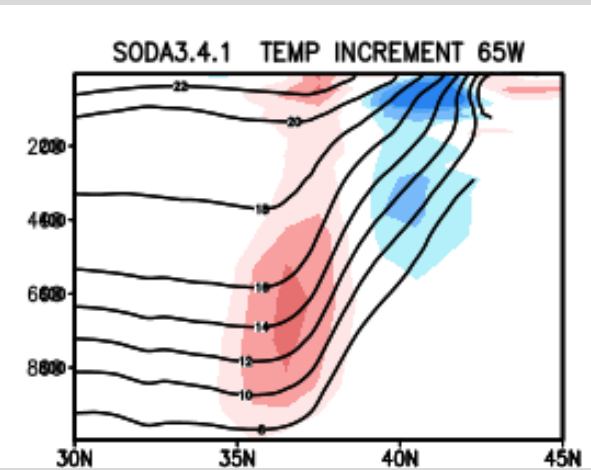
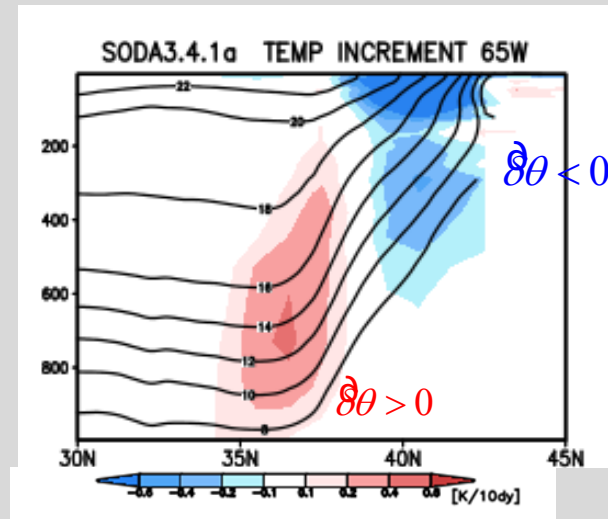
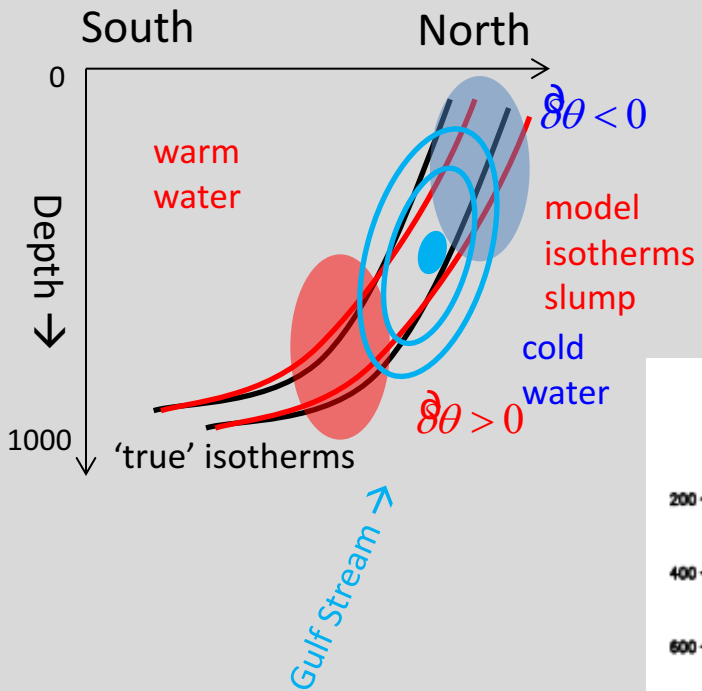
$h = 75m$

Before



Cross-section of temperature imbalance $\delta\theta$ across the Gulf Stream

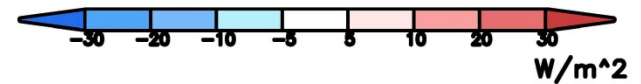
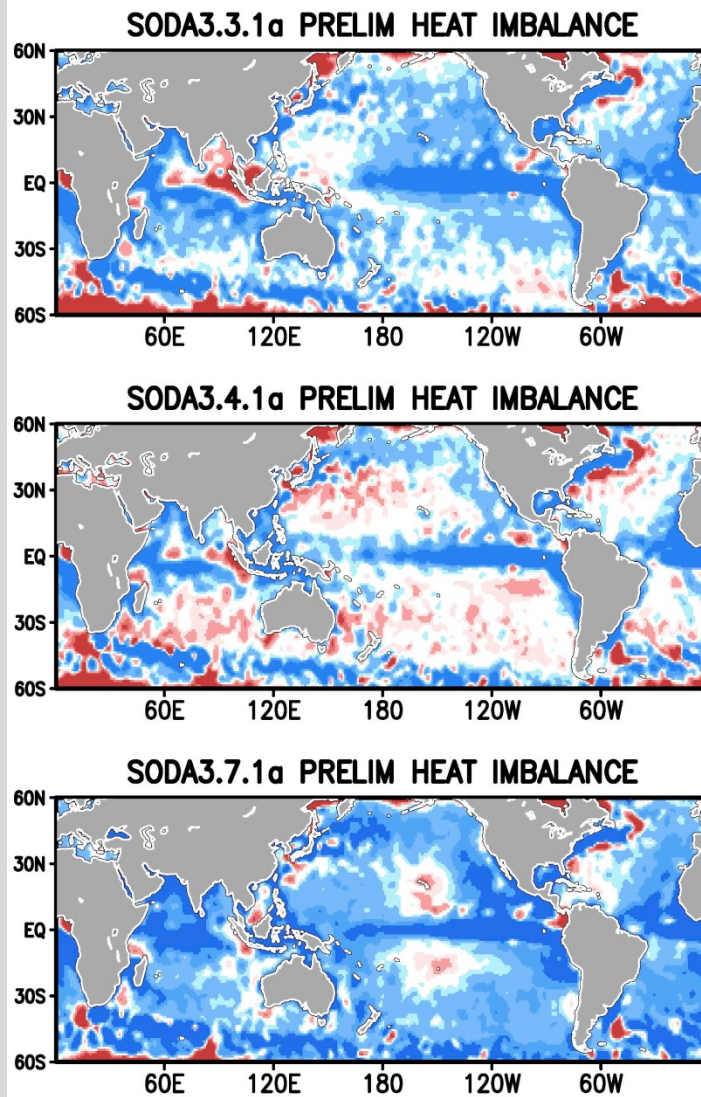
Cross-section along 65°W



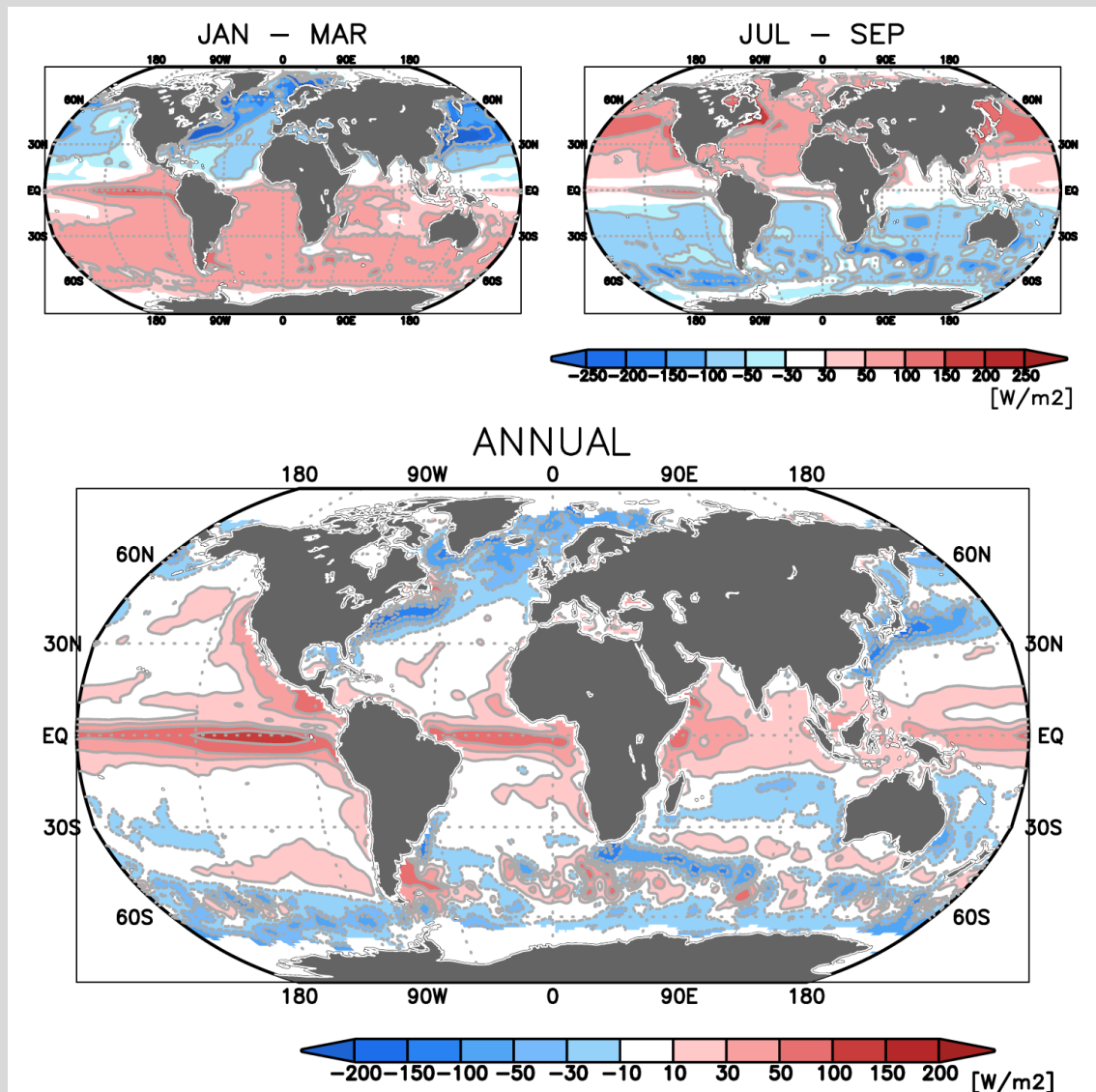
Three reanalyses

$$\frac{\partial}{\partial \theta} \frac{\rho C_p h}{\Delta t}$$

Before



Improved estimate of seasonal heat flux



Global imbalance:
 $\sim 3 \text{ Wm}^{-2}$

∞ Comments ∞

We argue in favor of using increments correct surface fluxes. It works great: it's cheap and iterative.

In playing with this approach we find:

- Most surface net heat flux misfit (error) is stored locally in the mixed layer – and it is mainly seasonal.
- Approach corrects seasonal heat fluxes to within $\pm 5 \text{ W m}^{-2}$ except in regions of strong currents.
- Approach also provides a way to evaluate
 - model error
 - Bulk flux parameterizations
 - Sea ice thickness